

CENTRE DE PHYSIQUE THÉORIQUE <sup>1</sup>  
CNRS–Luminy, Case 907  
13288 Marseille Cedex 9  
FRANCE

## Higgs-mass predictions

Thomas Schücker <sup>2</sup>

### Abstract

A compilation of Higgs-mass predictions is proposed.

PCAC-06: 14.80.Bn Standard-model Higgs boson

0708.3344

<sup>1</sup> Unité Mixte de Recherche (UMR 6207) du CNRS et des Universités Aix–Marseille 1 et 2 et Sud Toulon–Var, Laboratoire affilié à la FRUMAM (FR 2291)

<sup>2</sup> also at Université Aix–Marseille 1, [thomas.schucker@gmail.com](mailto:thomas.schucker@gmail.com)

# 1 Introduction

Many physicists hope that the electro-weak Higgs scalar will be observed within a few years at the LHC or at the Tevatron. The literature contains a plethora of predictions or upper limits of the Higgs mass based on many different ideas, models and calculational techniques. Privileged among them is the value  $m_H = 150 \pm 36$  GeV currently given by the LEP Electroweak Working Group, because it only relies on precision electro-weak data, non-observation of the Higgs today and the minimal hypothesis that the standard model is correct as it stands. A compilation of all other predictions is attempted here. Some models make additional predictions or postdictions, that are indicated. The point in time separating pre- and postdiction is taken as the time of publication of the model. In this task it is unavoidable that I will miss some references. I beg their authors' pardon and would like to ask them to kindly drop me a mail. Also some of the older pre- and postdictions might need an update due to changed experimental values of e.g. the top-mass, gauge couplings,... I would be happy to receive and to include such updates.

The predictions are organised in increasing order of the central value of the predicted mass interval. In a second section the upper limits are presented in increasing order as well. A third section contains a single lower limit. Older predictions and limits incompatible with today's experimental lower limit of 114 GeV are not recorded here. However, I should mention the supersymmetric model by Dermíšek & Gunion (2005) with a Higgs mass of 100 GeV. Because of exotic decay channels this model is still compatible with LEP data. Also not recorded are predictions that come with postdictions contradicting present experimental numbers.

The references are in alphabetical order of the first author's last name with chronology as secondary criterion.

## 2 Predictions

- $m_H = 109 \pm 12$  GeV

**Authors:** O. Buchmüller *et al.* (2007)

**Idea:** constrained minimal supersymmetric standard model combined with electro-weak precision data, flavor physics and abundance of cold dark matter

**Techniques:** multi-parameter fit, renormalisation group equation. The top mass is taken to be  $m_t = 170.9 \pm 1.8$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H = 115.3 \pm 0.1$  GeV

**Author:** Schücking (2007)

**Idea:** interpretation of the  $SU(2) \times U(1)$  group of the electro-weak forces as symmetry group of the Eguchi-Hanson metric

**Techniques:** differential geometry and quaternions

- $m_H = 117 \pm 4$  GeV

**Authors:** Gogoladze, Okada & Shafi (2007)

**Idea:** Higgs boson as zero mode of gauge boson along a fifth compactified dimension

**Techniques:** a boundary condition on the Higgs self-coupling at compactification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^8$  GeV

- $m_H = 118$

**Authors:** Arbuzov, Barbashov, Pervushin, Shuvalov & Zakharov (2008)

**Idea:** Three peaks of the cosmic microwave background are explained by the decay of primordial Higgs-,  $W$ - and  $Z$ -bosons into photons.

**Techniques:** conformal cosmology

**Other prediction:**  $m_H = 216$

- $m_H = 120 \pm 6$  GeV

**Authors:** Ellis, Nanopoulos, Olive & Santoso (2005)

**Idea:** supersymmetry

**Techniques:** minimal supersymmetric extension of the standard model with universal soft supersymmetry-breaking masses

**Other predictions:** many supersymmetric particles

- $m_H = 121 \pm 6$  GeV

**Authors:** Feldstein, Hall & Watari (2006)

**Idea:** superstring inspired landscape of vacua and some probability density for the parameters of the Higgs potential

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{19}$  GeV

**Postdiction:**  $m_t = 176 \pm 2$  GeV

- $m_H = 121.8 \pm 11$  GeV

**Authors:** Froggatt & Nielsen (1995)

**Idea:** two approximately degenerate vacua, one in which we live, the other of Planck energy

**Techniques:** renormalisation group equations

**Postdiction:**  $m_t = 173 \pm 4$  GeV

- $m_H = 122 \pm 10$  GeV

**Authors:** Djouadi, Heinemeyer, Mondragon & Zoupanos (2004)

**Idea:** a supersymmetric version of  $SU(5)$

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

**Postdictions:**  $m_t = 174 - 183$  GeV

- $m_H = 123.5 \pm 5.5$  GeV

**Authors:** Heinemeyer, M. Mondragon & G. Zoupanos (2007)

**Idea:** a supersymmetric Grand Unified Theory that can be made all-loop finite

**Techniques:** renormalisation group flow with  $m_t = 170.9$  GeV

**Other predictions:** supersymmetric particles

- $m_H = 124 \pm 21$  GeV

**Authors:** Barger, Deshpande, Jiang, Langacker & Li (2007)

**Idea:** supersymmetry broken at  $10^5 - 10^{16}$  GeV and gauge coupling unification at  $\Lambda \sim 10^{16} - 10^{17}$  GeV

**Techniques:** renormalisation group flow up to energies of  $\Lambda$

**Other predictions:** new vector-like fermions with masses in the 200 - 1000 GeV range

- $m_H = 124 \pm 10$  GeV

**Authors:** Arbuzov, Glinka, Lednicky & Pervushin (2007), version 6

**Idea:** condensates, conformal cosmology

**Techniques:** Coleman-Weinberg potential

**Other predictions:**  $m_H = 275 \pm 25$  GeV, version 1

- $m_H = 124.2 \pm 13.2$  GeV

**Authors:** Codoban, Jurcisin & Kazakov (1999)

**Idea:** supersymmetry

**Techniques:** minimal supersymmetric extension of the standard model with non-universal soft supersymmetry-breaking masses

**Other predictions:** many supersymmetric particles

- $m_H = 125 \pm 4$  GeV

**Authors:** Gogoladze, Okada & Shafi (2007)

**Idea:** Higgs boson as zero mode of gauge boson along a fifth compactified dimension

**Techniques:** a boundary condition on the Higgs self-coupling at compactification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{13} - 10^{14}$  GeV.

- $m_H = 126.3 \pm 2.2$  GeV

**Authors:** Shaposhnikov & C. Wetterich (2009)

**Idea:** Assume that gravity is asymptotically safe, that there are no intermediate energy scales between the Fermi and Planck scales, that the gravity induced anomalous dimension of the Higgs selfcoupling is positive.

**Techniques:** renormalisation group flow with  $m_t = 171.2$  GeV

- $m_H = 127.5 \pm 7.5$  GeV

**Authors:** Chankowski, Falkowski, Pokorski & Wagner (2004)

**Idea:** supersymmetry and the Higgs as a pseudo-Goldstone boson of some extra global symmetry

**Techniques:** smaller fine-tuning than in the minimal supersymmetric extension of the standard model. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 178 \pm 4.3$  GeV.

**Other predictions:** many supersymmetric particles and an additional  $Z$ -boson with a mass of 3 TeV

- $m_H = 129.6$  GeV

**Authors:** X. Calmet & H. Fritzsch (2001)

**Idea:** confining  $SU(2)$  and a ‘complementarity principle’

**Techniques:** 1-loop corrections

- $m_H = 130 \pm 6$  GeV

**Authors:** Dae Sung Hwang, Chang-Yeong Lee & Ne’eman (1996)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** renormalisation group flow

**Postdictions:**  $\sin^2 \theta_w = 0.229 \pm 0.005$

- $m_H = 131 \pm 10$  GeV

**Authors:** Gogoladze, Li, Senoguz & Shafi (2006)

**Idea:** 7 dimensional orbifold with  $SU(7)$  grand unification and split supersymmetry

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:**  $m_H = 146 \pm 8$  GeV

- $m_H = 134 \pm 9$  GeV

**Authors:** Ni, Lou, Lu & Yang (1998)

**Idea:** a Gaussian effective potential

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{15}$  GeV

- $m_H = 135 \pm 6$  GeV

**Authors:** Gogoladze, Li & Shafi (2006)

**Idea:** 7 dimensional  $N = 1$  supersymmetric orbifold with  $SU(7)$  grand unification

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:**  $m_H = 144 \pm 4$  GeV

- $m_H = 135 \pm 15$  GeV

**Authors:** Arkani-Hamed & Dimopoulos (2004)

**Idea:** split supersymmetry

**Techniques:** fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV

- $m_H = 137 \pm 23$  GeV

**Authors:** Medina, Shah & Wagner (2007)

**Idea:** a warped fifth dimension and an extension of the electro-weak gauge symmetry to  $SO(5) \times U(1)$  in the bulk, broken at the boundaries

**Techniques:** Coleman-Weinberg potential

- $m_H = 140 \pm 10$  GeV

**Authors:** Babu, Gogoladze, Rehman & Shafi (2008)

**Idea:** minimal supersymmetric extension of the standard model plus complete vectorlike multiplets of grand unified groups

**Techniques:** some fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV. The top mass is taken to be  $m_t = 172.6 \pm 1.4$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H = 141 \pm 2$  GeV

**Authors:** Hall & Y. Nomura (2009)

**Idea:** minimal supersymmetric extension of the standard model plus supersymmetry breaking at very high scale, motivated from a multiverse

**Techniques:** huge fine tuning and 2-loop corrections with a top mass of 173.1 GeV

**Other predictions:** no supersymmetric particles

- $m_H = 143 \pm 37$  GeV

**Authors:** Cabibbo, Maiani, Parisi & Petronzio (1979)

**Idea:** the big desert: no new particles besides the Higgs and validity of perturbative

quantum field theory up to the Planck scale

**Techniques:** renormalisation group flow up to energies of  $10^{19}$  GeV. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 171.5 \pm 2$  GeV.

- $m_H = 143.2 \pm 28.8$  GeV

**Authors:** Gogoladze, Okada & Shafi (2007.2)

**Idea:** 2 extra dimensions compactified on an orbifold

**Techniques:** a boundary condition on the Higgs self-coupling at compactification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{19}$  GeV.

- $m_H = 144 \pm 4$  GeV

**Authors:** Gogoladze, Li & Shafi (2006)

**Idea:** 7 dimensional  $N = 1$  supersymmetric orbifold with  $SU(7)$  grand unification

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV.

**Other predictions:**  $m_H = 135 \pm 6$  GeV

- $m_H = 145 \pm 7$  GeV

**Author:** Liu (2005)

**Idea:** supersymmetry broken at  $10^{11}$  GeV and a  $\mathbb{Z}_3$  symmetry among generations

**Techniques:** radiative corrections

- $m_H = 146 \pm 8$  GeV

**Authors:** Gogoladze, Li, Senoguz & Shafi (2006)

**Idea:** 7 dimensional orbifold with  $SU(7)$  grand unification and split supersymmetry

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV.

**Other predictions:**  $m_H = 131 \pm 10$  GeV

- $m_H = 146 \pm 19$  GeV

**Authors:** Barger, Jiang, Langacker & Li (2005)

**Idea:** supersymmetry broken at high scale and gauge coupling unification at  $\Lambda \sim 10^{16} - 10^{17}$  GeV

**Techniques:** renormalisation group flow up to energies of  $\Lambda$

- $m_H = 148.1 \pm 10.7$  GeV

**Author:** Popa (2009)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action with  $m_t = 171.3$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 150 \pm 36$  GeV

**Authors:** The LEP Electroweak Working Group

**Idea:** non-observation of the Higgs and quantum corrections by Higgs loops to precision electro-weak data

**Techniques:** experiment and quantum field theory

- $m_H = 150 \pm 10$  GeV

**Authors:** Barger, Chiang, Jiang & Li (2004)

**Idea:** supersymmetry broken at  $10^{11}$  GeV and Peccei-Quinn symmetry

**Techniques:** radiative corrections

- $m_H = 150 \pm 20$  GeV

**Authors:** Arvanitaki, Davis, Graham & Wacker (2004)

**Idea:** split supersymmetry

**Techniques:** fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV

- $m_H = 150 \pm 50$  GeV

**Authors:** Bai, Fan & Han (2007)

**Idea:** supersymmetry and a long-lived metastable supersymmetry breaking vacuum

**Techniques:** little Higgs mechanism, 1-loop corrections

**Other predictions:** many supersymmetric particles plus new gauge bosons and electro-weak triplets at 1 TeV

- $m_H = 150 \pm 24$  GeV

**Authors:** Shaposhnikov & C. Wetterich (2009)

**Idea:** Assume that gravity is asymptotically safe, that there are no intermediate energy scales between the Fermi and Planck scales.

**Techniques:** renormalisation group flow with  $m_t = 171.2$  GeV

- $m_H = 153 \pm 3$  GeV

**Author:** Okumura (1997)

**Idea:** a vague variant of the Connes-Lott model

**Techniques:** 2-loop renormalisation group flow up to energies of  $10^{13}$  GeV. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 171.5 \pm 2$  GeV.

- $m_H = 154 \pm 6$  GeV

**Authors:** Ananthanarayan & Pasupathy (2001)

**Idea:** weak dependence of the ratio between Higgs self-coupling and top Yukawa coupling squared on renormalisation scale

**Techniques:** 1- and 2-loop corrections

- $m_H = 155 \pm 8$  GeV

**Author:** Schrempp & Schrempp (1993)

**Idea:** A strongly infrared attractive line in the  $m_t - m_H$  plane is found.

**Techniques:** 1-loop renormalization group equations

- $m_H = 160 \pm 8$  GeV

**Authors:** Roepstorff & Vehns (2000)

**Idea:** combining gauge and Yukawa interactions in one generalised Dirac operator

**Techniques:** superconnections

**Postdictions:**  $m_t = 160 \pm 8$  GeV

- $m_H = 160 \pm 20$  GeV

**Authors:** Langacker, Paz, Wang & Yavin (2007)

**Idea:** an extension of the minimal supersymmetric extension of the standard model plus a hidden sector plus a  $Z'$  mediating supersymmetry breaking by couplings to the hidden

sector

**Techniques:** 2-loop corrections up to energies of  $10^7 - 10^{11}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H = 160 \pm 24.5$  GeV

**Authors:** Barvinsky, Kamenshchik, Kiefer, Starobinsky & Steinwachs (2009)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 1-loop with  $m_t = 171$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160 \pm 30$  GeV

**Author:** Bezrukov (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160 \pm 34$  GeV

**Authors:** Bezrukov & Shaposhnikov (2009)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 2-loop with  $m_t = 171.2$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160.7 \pm 24$  GeV

**Authors:** Bezrukov, Magnin & Shaposhnikov (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 1-loop with  $m_t = 171$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160.9 \pm 0.1$  GeV

**Author:** Ne'eman (1986)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** classical field theory

**Postdictions:**  $\sin^2 \theta_w = 1/4$

- $m_H = 161.8033989$  GeV

**Author:** El Naschie (2005)

**Idea:** E-infinity theory

**Techniques:** ?

- $m_H = 170 \pm 10$  GeV

**Authors:** Chamseddine & Connes (1996)

**Idea:** derivation of the standard model from gravity by generalising Riemannian to non-commutative geometry



**Techniques:** operator algebras, heat-kernel expansion and renormalisation group flow up to energies of  $\Lambda \sim 10^{13} - 10^{17}$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 170.9 \pm 2.5$  GeV.

**Other predictions:** conceptual uncertainty in proper time measurements of  $\Delta\tau \sim \hbar/\Lambda = 10^{-41} - 10^{-37}$  s

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings,  $m_t < 186.3$  GeV.

- $m_H = 177.5 \pm 7.5$  GeV

**Authors:** Antusch, Kersten, Lindner & Ratz (2002)

**Idea:** the Higgs as a composite particle from neutrino condensation

**Techniques:** seesaw mechanism, gap equation, renormalisation group flow up to the condensation scale  $\Lambda = 10^{16}$  GeV

- $m_H = 182 \pm 4$  GeV

**Author:** Namsrai (1996)

**Idea:** Higgs mass from space-time curvature

**Techniques:** general relativity and solitons

- $m_H = 185 \pm 5$  GeV

**Author:** Schrempp & Schrempp (1986)

**Idea:** A largely unspecified strong interaction is assumed to soften the elastic scattering of longitudinally polarised  $W$  bosons.

**Techniques:** a superconvergence sum rule

- $m_H = 185.7 \pm 0.1$  GeV

**Author:** Trostel (1987)

**Idea:** a geometrisation of the Yukawa couplings

**Techniques:** spinor connections

- $m_H = 186 \pm 8$  GeV

**Authors:** Tolksdorf & Thumstädter (2006)

**Idea:** differential geometric unification of general relativity and the standard model

**Techniques:** generalised Dirac operators, heat kernel expansion and renormalisation group flow up to energies of  $\Lambda \sim 10^{10}$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 174 \pm 3$  GeV.

- $m_H = 194 \pm 80$  GeV

**Authors:** García-Bellido, Figueroa & Rubio (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background, lower limit from non-observation of the Higgs at LEP

- $m_H = 197.2 \pm 124.8$  GeV

**Authors:** Froggatt, Laperashvili, Nevzorov, Nielsen & Sher (2006)

**Idea:** non-supersymmetric extension of the standard model with two Higgs doublets and

the multiple point principle

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^4 - 10^{19}$  GeV

**Other predictions:** additional neutral and charged scalars with masses larger than 202.4 GeV

- $m_H = 200 \pm 20$  GeV

**Authors:** Froggatt, Nevzorov, Nielsen & Thompson (2008)

**Idea:** non-supersymmetric extension of the standard model with two Higgs doublets and the multiple point principle

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^5$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 171.4 \pm 2.1$  GeV.

**Other predictions:** enhanced top-Higgs coupling

- $m_H = 200 \pm 50$  GeV

**Author:** Cvetič (1995)

**Idea:** It is supposed that the 1-loop contributions of the scalar self-interactions to the effective potential are distinctly less than those of the Yukawa couplings of the top.

**Techniques:** 1-loop corrections with cut-off at  $10^3$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 180$  GeV.

- $m_H = 203 \pm 2.2$  GeV

**Author:** Squellari & Stephan (2007)

**Idea:** extension of Chamseddine and Connes' spectral action to include three vectorlike isospin doublets

**Techniques:** operator algebras, heat-kernel expansion and renormalisation group flow up to  $\Lambda = 3 - 5 \cdot 10^7$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 170.9 \pm 2.6$  GeV.

**Other predictions:** six new leptons with masses of 10–550 TeV, conceptual uncertainty in proper time measurements of  $\Delta\tau \sim \hbar/\Lambda \sim 10^{-32}$  s

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings.

- $m_H = 210 \pm 10$  GeV

**Authors:** Andrianov & Romanenko (1995)

**Idea:** modified Veltman condition and fixed point in running of Yukawa coupling

**Techniques:** renormalisation group flow up to energies of  $10^{16}$  GeV

**Postdictions:**  $m_t = 175 \pm 5$  GeV

- $m_H = 216$

**Authors:** Arbuzov, Barbashov, Pervushin, Shuvalov & Zakharov (2008)

**Idea:** Three peaks of the cosmic microwave background are explained by the decay of primordial Higgs-,  $W$ - and  $Z$ -bosons into photons.

**Techniques:** conformal cosmology

**Other prediction:**  $m_H = 118$

- $m_H = 226 \pm 50$  GeV

**Authors:** Aranda, Díaz-Cruz & Rosado (2005)

**Idea:** unification of the weak gauge couplings at intermediate energy  $\Lambda$  and linear or

quadratic relation of these to the Higgs self-coupling

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{13}$  GeV

- $m_H = 241.2 \pm 1.6$  GeV

**Author:** Stephan (2007)

**Idea:** extension of Chamseddine and Connes' spectral action to  $SU(4) \times SU(3) \times SU(2) \times U(1)$

**Techniques:** operator algebras, heat-kernel expansion and renormalisation group flow up to  $\Lambda = 2 \cdot 10^4$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 170.9 \pm 2.6$  GeV.

**Other predictions:** confined  $SU(4)$  singlets in the TeV range, conceptual uncertainty in proper time measurements of  $\Delta\tau \sim \hbar/\Lambda = 3.3 \cdot 10^{-29}$  s

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings.

- $m_H = 250 \pm 50$  GeV

**Authors:** Barbieri, Hall, Nomura & Rychkov (2006)

**Idea:** extending the minimal supersymmetric extension of the standard model by adding a chiral singlet with a superpotential interaction with the Higgs doublets

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10$  TeV

- $m_H \approx 250$  GeV

**Authors:** Ne'eman & Thierry Mieg (1982)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** classical field theory

**Postdictions:**  $\sin^2 \theta_w = 1/4$

- $m_H = 255 \pm 145$  GeV

**Author:** Mahbubani (2004)

**Idea:** split supersymmetry

**Techniques:** fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV

- $m_H = 271 \pm 5$  GeV

**Authors:** Connes & Lott (1991)

**Idea:** derivation of the Higgs sector of the standard model from the Yang-Mills sector by generalising Euclidean to noncommutative geometry

**Techniques:** operator algebras. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings,  $m_t > 139.3$  GeV,  $\sin^2 \theta_w < 0.543$ .

- $m_H = 275 \pm 25$  GeV

**Authors:** Arbuzov, Glinka, Lednický & Pervushin (2007), version 1

**Idea:** condensates, conformal cosmology

**Techniques:** Coleman-Weinberg potential

**Other predictions:**  $m_H = 124 \pm 10$  GeV, version 6

- $m_H = 308.6 \pm 0.3$  GeV

**Authors:** López Castro & Pestieau (1995)

**Idea:** absence of quadratic and logarithmic divergences in the top mass

**Techniques:** 1-loop quantum corrections

**Other predictions:**  $m_t = 170.5 \pm 0.3$  GeV

- $m_H = 309 \pm 6$  GeV

**Authors:** Decker & Pestieau (1979), also Veltman (1981)

**Idea:** absence of quadratic 1-loop divergences

**Techniques:** dimensional reduction. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

- $m_H = 317 \pm 80$  GeV

**Authors:** Bazzocchi & Fabbrichesi (2004)

**Idea:** Flavour symmetry broken together with electro-weak symmetry, little Higgs

**Techniques:** Coleman-Weinberg effective potential

**Other predictions:** Many new particles including a charged scalar with mass  $560 \pm 192$  GeV

- $m_H = 374 \pm 6$  GeV

**Author:** Xiao-Gang He (2002)

**Idea:** no dependence of total vacuum energy (Casimir plus minimum of Higgs potential) on renormalisation scale

**Techniques:** Casimir effect and quantum corrections. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

- $m_H = 426$  GeV

**Author:** Fairlie (1979)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** classical field theory

**Postdictions:**  $\sin^2 \theta_w = 1/4$

- $m_H = 500 \pm 100$  GeV

**Authors:** Barbieri, Hall & Rychkov (2006)

**Idea:** adding an inert isospin doublet of pseudo scalars

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 1.5$  TeV

**Other predictions:** pseudo scalars with masses between 60 GeV and 1 TeV leading in particular to an increased width of the ordinary Higgs scalar

- $m_H = 515 \pm 64$  GeV

**Authors:** Langguth, Montvay & Weisz (1986)

**Idea:** lattice gauge theory and triviality of the continuum limit

**Techniques:** Monte Carlo simulations on  $12^4$  lattices

- $m_H = 536 \pm 10$  GeV

**Authors:** Babic, Guberina, Horvat & Stefancic (2001)

**Idea:** no dependence of cosmological constant on renormalisation scale

**Techniques:** quantum corrections. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

- $m_H = 760 \pm 21$  GeV

**Authors:** Cea, Consoli & Cosmai (2003)

**Idea:** lattice gauge theory and triviality of the continuum limit

**Techniques:** extrapolation from Ising limit

- $m_H = 1900 \pm 100$  GeV

**Authors:** Ibañez-Meier & Stevenson (1992)

**Idea:** vanishing bare Higgs mass and 1-loop effective potential

**Techniques:** autonomous renormalisation

- $m_H = 10^{18}$  GeV

**Authors:** Batakis & Kehagias (1991)

**Idea:** Higgs field as massive excitation of the vacuum configuration of a sigma field coupled to gravity

**Techniques:** non-linear sigma models

### 3 Upper bounds

- $m_H < 123$  GeV

**Authors:** Belyaev, Dar, Gogoladze, Mustafayev & Shafi (2007)

**Idea:** constrained minimal supersymmetric standard model combined with supersymmetry constraints from colliders and low energy physics and constraints on dark matter

**Techniques:** renormalisation group equation. The top mass is taken to be  $m_t = 171.4$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H < 125$  GeV

**Authors:** Froggatt, Nevzorov, Nielsen & Thompson (2008)

**Idea:** non-supersymmetric extension of the standard model with two Higgs doublets and the multiple point principle

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{10}$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 171.4 \pm 2.1$  GeV.

- $m_H < 125$  GeV

**Authors:** Babu, Gogoladze, Rehman & Shafi (2008)

**Idea:** minimal supersymmetric extension of the standard model plus complete vectorlike multiplets of grand unified groups

**Techniques:** some fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV. The top mass is taken to be  $m_t = 172.6 \pm 1.4$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H < 126$  GeV

**Authors:** De Simone, Hertzberg & Wilczek (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 2-loop with  $m_t = 171.2$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave

## Background

- $m_H < 127$  GeV

**Authors:** Carena, Nardini, Quiros & Wagner (2008)

**Idea:** minimal supersymmetric extension of the standard model with a light stop and electro-weak baryo-genesis

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** the light stop with mass  $< 120$  GeV

- $m_H < 130$  GeV

**Authors:** Okada, Yamaguchi & Yanagida (1991)

**Idea:** minimal supersymmetric extension of the standard model

**Techniques:** soft supersymmetry breaking at 1 TeV and quantum corrections

**Other predictions:** many supersymmetric particles

- $m_H < 130$  GeV

**Authors:** Bento, Bertolami & Rosenfeld (2001)

**Idea:** introduction of a stable gauge singlet scalar of mass around 1 GeV coupled to the Higgs, playing the role of cold dark matter and solving problems with small scale structure formation

**Techniques:** phenomenological constraints from cosmology and particle physics

**Other predictions:** Higgs decay into a pair of these stable light scalars

- $m_H < 130$  GeV

**Authors:** Birkedal, Chacko & Gaillard (2004)

**Idea:** supersymmetry and the Higgs as a pseudo-Goldstone boson of some extra global symmetry

**Techniques:**  $SU(6)$  grand unification

**Other predictions:** many supersymmetric particles

- $m_H < 130$  GeV

**Authors:** Passera, Marciano & Sirlin (2008)

**Idea:** hypothetical errors in the determination of the hadronic leading-order contribution to cure the present discrepancy between experiment and prediction of the muon  $g - 2$

**Techniques:** quantum corrections by Higgs loops to precision electro-weak data with  $m_t = 172.6 \pm 1.4$  GeV

- $m_H < 139$  GeV

**Authors:** Kaeding & Nandi (1999)

**Idea:** a non-minimal supersymmetric extension of the standard model

**Techniques:** gauge mediated supersymmetry breaking and quantum corrections

**Other predictions:** many supersymmetric particles

- $m_H < 144$  GeV

**Authors:** Suematsu & Zoupanos (2001)

**Idea:** a non-minimal supersymmetric extension of the standard model

**Techniques:** non-universal soft supersymmetry breaking and quantum corrections

**Other predictions:** many supersymmetric particles

- $m_H < 150$  GeV

**Authors:** Maloney, Pierce & Wacker (2004)

**Idea:** supersymmetric extension of the standard model with non-decoupling D-terms

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles and new gauge bosons with masses in the TeV range

- $m_H < 150$  GeV

**Authors:** Moroi & Okada (1992)

**Idea:** supersymmetric extension of the standard model plus a gauge singlet

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 150$  GeV

**Authors:** Carena, Nardini, Quiros & Wagner (2008)

**Idea:** minimal supersymmetric extension of the standard model with a light stop

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** the light stop

- $m_H < 165$  GeV

**Authors:** Delgado & Quiros (2000)

**Idea:** supersymmetric extension of the standard model plus one extra dimension compactified on an orbifold

**Techniques:** renormalisation group flow with all Higgses in the bulk

**Other predictions:** many supersymmetric particles

- $m_H < 180$  GeV

**Authors:** Moroi & Okada (1992)

**Idea:** supersymmetric extension of the standard model plus extra matter multiplets

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 200$  GeV

**Authors:** Espinosa & Quiros (1998)

**Idea:** supersymmetric extension of the standard model plus extra matter multiplets

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 230$  GeV

**Authors:** Bhattacharyya, Majee & Raychaudhuri (2007)

**Idea:** supersymmetric extension of the standard model plus one extra dimension

**Techniques:** Kaluza-Klein and radiative corrections

- $m_H < 235$  GeV

**Authors:** Bhattacharyya, Majee & Ray (2008)

**Idea:** supersymmetric extension of the standard model plus one extra dimension, Higgs confined to the TeV brane

**Techniques:** Kaluza-Klein and radiative corrections

- $m_H < 260$  GeV

**Authors:** Batra, Delgado, Kaplan & Tait (2004)

**Idea:** supersymmetric extension of the standard model plus a gauge singlet

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles and a charged Higgs boson lighter than the neutral one

- $m_H < 350$  GeV

**Authors:** Batra, Delgado, Kaplan & Tait (2003)

**Idea:** supersymmetric extension of the standard model plus some new gauge bosons

**Techniques:** soft supersymmetry breaking, some fine tuning

**Other predictions:** many supersymmetric particles and new gauge bosons with masses in the TeV range

- $m_H < 400$  GeV

**Authors:** Litsey & M. Sher (2009)

**Idea:** minimal supersymmetric extension of the standard model with a fourth generation

**Techniques:** radiative corrections

**Other predictions:** the fourth generation at LHC energies and many supersymmetric particles

- $m_H < 446$  GeV

**Authors:** Huitu, Pandita & Puolamaki (1997)

**Idea:** supersymmetric extension of the left-right symmetric extension of the standard model

**Techniques:** soft supersymmetry breaking, 1-loop corrections

- $m_H < 450$  GeV

**Authors:** Bhattacharyya, Majee & Raychaudhuri (2007)

**Idea:** supersymmetric extension of the standard model plus two extra dimensions

**Techniques:** Kaluza-Klein and radiative corrections

- $m_H < 724$  GeV

**Authors:** Langguth & Montvay (1987)

**Idea:** lattice gauge theory and triviality of the continuum limit

**Techniques:** Monte Carlo simulations on  $16^4$  lattices

- $m_H < 800$  GeV

**Authors:** Appelquist & Yee (2002)

**Idea:** Kaluza-Kein with one or two extra compactified dimensions

**Techniques:** computation of quantum corrections induced by Kaluza-Klein particles on precision electro-weak measurements of the flavour changing process  $b \rightarrow s + \gamma$  and on



the anomalous magnetic moment of the muon

**Other predictions:** new dimensions with inverse compactification radius as low as 250 GeV

- $m_H < 880$  GeV

**Authors:** Jegerlehner, Kalmykov & Veretin (2001)

**Idea:** Quantum corrections in the relation between  $\overline{\text{MS}}$ - and pole-masses of the  $W$ - and  $Z$ -bosons should remain perturbative.

**Techniques:** 2-loop corrections, asymptotic expansions

- $m_H < 1400$  GeV

**Authors:** Grzadkowski & Gunion (2007)

**Idea:**  $W^+W^-$  scattering in the Randall-Sundrum model with one extra dimension and two 3-branes should remain perturbatively unitary after inclusion of string/M-theoretic excitations.

**Techniques:** summation of Kaluza-Klein gravitons

## 4 A lower bound

- $m_H > 230$  GeV

**Authors:** Barvinsky, Kamenshchik & Starobinsky (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

## 5 Final remarks

Our present list contains 78 Higgs-mass predictions. Supersymmetry is behind 23 of them. With the exception of two ( $250 \pm 50$  GeV,  $255 \pm 145$  GeV), their central values lie between 120 and 160 GeV. Compactified additional dimensions motivate eight predictions ranging from 117 to 146 GeV. There is one prediction from a superstring inspired landscape: 121 GeV. The embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$  produces four predictions: 130, 161, 250 and 426 GeV. One prediction, 178 GeV, is motivated by dynamical symmetry breaking via a neutrino condensate. We have listed four predictions from Connes's noncommutative geometry: 170, 203, 241 and 271 GeV. Lattice gauge theories lead to two predictions: 515 and 760 GeV. Eight predictions are based on the (approximate) vanishing of particular terms related to quantum corrections: 154, 155, 200, 210, 309, 374 and 536 GeV. The following three intervals are still free of Higgs-mass predictions:  $600 - 739$  GeV,  $781 - 1800$  GeV and  $2000 - 10^{18}$  GeV.

We have 28 upper bounds for the Higgs mass, 20 of which come from supersymmetry.

Five predictions, one upper and one lower bound come from the recent idea that

inflation is driven by the Higgs scalar together with a strong non-minimal coupling to gravity. The Higgs mass is obtained from fitting the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background.

In this compilation we have only considered numerical pre- and postdictions. Today particle physicists are used to interpret experimental numbers not only in terms of numbers like coupling constants, but also in terms of groups and representations and even in terms of Lagrangians. Only few of the listed models come with constraints on groups, representations and Lagrangians. Supersymmetric models for instance need representations for supersymmetric particles and thereby may be falsified by the LHC. However supersymmetry does not constrain the gauge group nor the Lagrangian. This is different for Connes' noncommutative geometry, which — just as Riemannian geometry — puts severe constraints on the admissible Lagrangians, puts constraints on gauge groups and severe constraints on representations. In particular the Higgs representation of the noncommutative standard model is not chosen but computed to be one colourless isospin doublet. This is certainly its most startling and robust prediction and may lead to its falsification if more than one physical Higgs is found as predicted by any supersymmetric standard model.

## References

- [1] The LEP Electroweak Working Group, <http://lepewwg.web.cern.ch>, 150 GeV
- [2] A. A. Andrianov & N. V. Romanenko, *Vacuum Fine Tuning And Masses Of The T Quark And Higgs Boson*, Phys. Lett. B343 (1995) 295, 210 GeV
- [3] S. Antusch, J. Kersten, M. Lindner & M. Ratz, *Dynamical electroweak symmetry breaking by a neutrino condensate*, hep-ph/0211385, Nucl. Phys. B658 (2003) 203, 177.5 GeV
- [4] T. Appelquist & Ho-Ung Yee, *Universal extra dimensions and the Higgs boson mass*, hep-ph/0211023, Phys. Rev. D67 (2003) 055002, < 800 GeV
- [5] A. Aranda, J. L. Díaz-Cruz & A. Rosado, *Electroweak-Higgs unification and the Higgs boson mass*, hep-ph/0507230, Int. J. Mod. Phys. A22 (2007) 1417, 226 GeV
- [6] A. B. Arbuzov, L. A. Glinka, R. Lednicky & V. N. Pervushin, *Higgs Particle Mass in Cosmology*, arXiv:0705.4672, 124 and 275 GeV
- [7] A. B. Arbuzov, B. M. Barbashov, V. N. Pervushin, S. A. Shuvalov & A. F. Zakharov, *Is it possible to estimate the Higgs Mass from the CMB Power Spectrum?*, arXiv:0802.3427, 118 and 216 GeV
- [8] N. Arkani-Hamed & S. Dimopoulos, *Supersymmetric unification without low energy supersymmetry and signatures for fine-tuning at the LHC*, hep-th/0405159, JHEP 0506 (2005) 073, 135 GeV

- [9] A. Arvanitaki, C. Davis, P. W. Graham & J. G. Wacker, *One loop predictions of the finely tuned SSM*, hep-ph/0406034, Phys. Rev. D70 (2004) 117703, 150 GeV
- [10] A. Babic, B. Guberina, R. Horvat & H. Stefancic, *Renormalization-group running of the cosmological constant and its implication for the Higgs boson mass in the standard model*, hep-ph/0111207 Phys. Rev. D65 (2002) 085002, 536 GeV
- [11] K. S. Babu, I. Gogoladze, M. U. Rehman & Q. Shafi, *Higgs Boson Mass, Sparticle Spectrum and Little Hierarchy Problem in Extended MSSM*, arXiv:0807.3055, 140 GeV, < 125 GeV
- [12] Y. Bai, J. Fan & Z. Han, *Higgs boson from the meta-stable SUSY breaking sector*, arXiv:0706.0007, 150 GeV
- [13] R. Barbieri, L. J. Hall & V. S. Rychkov, *Improved naturalness with a heavy Higgs: An alternative road to LHC physics*, hep-ph/0603188, Phys. Rev. D74 (2006) 015007, 500 GeV
- [14] R. Barbieri, L. J. Hall, Y. Nomura & V. S. Rychkov, *Supersymmetry without a light Higgs boson*, hep-ph/0607332, Phys. Rev. D75 (2007) 035007, 250 GeV
- [15] V. Barger, C. W. Chiang, J. Jiang & T. Li, *Axion models with high-scale supersymmetry breaking*, hep-ph/0410252, Nucl. Phys. B705 (2005) 71, 150 GeV
- [16] V. Barger, J. Jiang, P. Langacker & T. Li, *Gauge coupling unification in the standard model*, hep-ph/0503226, Phys. Lett. B624 (2005) 233  
*Non-canonical gauge coupling unification in high-scale supersymmetry breaking*, hep-ph/0504093, Nucl. Phys. B726 (2005) 149, 146 GeV
- [17] V. Barger, N. G. Deshpande, J. Jiang, P. Langacker & T. Li, *Implications of canonical gauge coupling unification in high-scale supersymmetry breaking*, hep-ph/0701136, 124 GeV
- [18] A. O. Barvinsky, A. Y. Kamenshchik & A. A. Starobinsky, *Inflation scenario via the Standard Model Higgs boson and LHC*, arXiv:0809.2104 [hep-ph], JCAP 0811 (2008) 021, > 230 GeV
- [19] A. O. Barvinsky, A. Y. Kamenshchik, C. Kiefer, A. A. Starobinsky & C. Steinwachs, *Asymptotic freedom in inflationary cosmology with a non-minimally coupled Higgs field*, arXiv:0904.1698 [hep-ph], JCAP 0912 (2009) 003, 160 GeV
- [20] N. A. Batakis & A. A. Kehagias, *Higgs mass determined in the gravity coupled sigma model*, Phys. Lett. B253 (1991) 149,  $10^{18}$  GeV
- [21] P. Batra, A. Delgado, D. E. Kaplan & T. M. P. Tait, *The Higgs mass bound in gauge extensions of the minimal supersymmetric standard model*, hep-ph/0309149, JHEP 0402 (2004) 043, < 350 GeV

- [22] P. Batra, A. Delgado, D. E. Kaplan & T. M. P. Tait, *Running into new territory in SUSY parameter space*, hep-ph/0404251, JHEP 0406 (2004) 032,  $< 260$  GeV
- [23] F. Bazzocchi & M. Fabbri, *A Heavy Higgs boson from flavor and electroweak symmetry breaking unification*, hep-ph/0407358, Phys. Rev. D70 (2004) 115008, 317 GeV
- [24] A. Belyaev, S. Dar, I. Gogoladze, A. Mustafayev & Q. Shafi, *Interplay of Higgs and Sparticle Masses in the CMSSM with updated SUSY constraints*, arXiv:0712.1049,  $< 123$  GeV
- [25] M. C. Bento, O. Bertolami & R. Rosenfeld, *Cosmological constraints on an invisibly decaying Higgs boson*, hep-ph/0103340, Phys. Lett. B518 (2001) 276,  $< 130$  GeV
- [26] F. L. Bezrukov, *The Standard model Higgs as the inflaton*, arXiv:0805.2236 [hep-ph], 160 GeV
- [27] F. L. Bezrukov, A. Magnin & M. Shaposhnikov, *Standard Model Higgs boson mass from inflation*, arXiv:0812.4950 [hep-ph], Phys. Lett. B 675 (2009) 88, 160.7 GeV
- [28] F. Bezrukov & M. Shaposhnikov, *Standard Model Higgs boson mass from inflation: two loop analysis*, arXiv:0904.1537 [hep-ph], JHEP 0907 (2009) 089, 160 GeV
- [29] G. Bhattacharyya, S. K. Majee & A. Raychaudhuri, *Extra-dimensional relaxation of the upper limit of the lightest supersymmetric neutral Higgs mass*, arXiv:0705.3103,  $< 230$  and  $< 450$  GeV
- [30] G. Bhattacharyya, S. K. Majee & T. S. Ray, *Radiative correction to the lightest neutral Higgs mass in warped supersymmetry*, arXiv:0806.3672,  $< 235$  GeV
- [31] A. Birkedal, Z. Chacko & M. K. Gaillard, *Little supersymmetry and the supersymmetric little hierarchy problem*, hep-ph/0404197, JHEP 0410 (2004) 036,  $< 130$  GeV
- [32] O. Buchmüller *et al.*, *Prediction for the Lightest Higgs Boson Mass in the CMSSM using Indirect Experimental Constraints*, arXiv:0707.3447, Phys. Lett. B657 (2007) 87, 109 GeV
- [33] N. Cabibbo, L. Maiani, G. Parisi & R. Petronzio, *Bounds on the fermions and Higgs boson masses in grand unified theories*, Nucl. Phys. B158 (1979) 295, 143 GeV
- [34] X. Calmet & H. Fritzsch, *Calculation of the Higgs boson mass using the complementarity principle*, hep-ph/0107085, Phys. Lett. B525 (2002) 297, 129.6 GeV
- [35] M. Carena, G. Nardini, M. Quiros & C. E. M. Wagner, *The Effective Theory of the Light Stop Scenario*, arXiv:0806.4297, JHEP 0810 (2008) 062,  $< 150$  GeV
- [36] M. Carena, G. Nardini, M. Quiros & C. E. M. Wagner, *The Baryogenesis Window in the MSSM*, arXiv:0809.3760, Nucl. Phys. B812 (2009) 243,  $< 127$  GeV

- [37] P. Cea, M. Consoli & L. Cosmai, *Indications on the Higgs boson mass from lattice simulations*, hep-lat/0309050 Nucl. Phys. Proc. Suppl. 129 (2004) 780, 760 GeV  
P. Cea & L. Cosmai, *The Higgs boson: from the lattice to LHC*, arXiv:0911.5220 [hep-ph], 754 GeV
- [38] A. Chamseddine & A. Connes, *The spectral action principle*, hep-th/9606001, Comm. Math. Phys. 182 (1996) 155  
A. Chamseddine, A. Connes & M. Marcolli, *Gravity and the standard model with neutrino mixing*, hep-th/0610241, Adv. Theor. Math. Phys. 11 (2007) 991, 170 GeV
- [39] P. H. Chankowski, A. Falkowski, S. Pokorski & J. Wagner, *Electroweak symmetry breaking in supersymmetric models with heavy scalar superpartners*, hep-ph/0407242, Phys. Lett. B598 (2004) 252, 127.5 GeV
- [40] S. Codoban, M. Juncisin & D. Kazakov, *Higgs mass prediction with non-universal soft supersymmetry breaking in MSSM*, hep-ph/9912504, Phys. Lett. B477 (2000) 223, 124.2 GeV
- [41] A. Connes & J. Lott, *The metric aspect of noncommutative geometry*, in the proceedings of the 1991 Cargèse Summer Conference, eds.: J. Fröhlich et al., Plenum Press (1992)  
D. Kastler & T. Schücker, *The standard model à la Connes-Lott*, hep-th/9412185, J. Geom. Phys. 24 (1997) 1, 271 GeV
- [42] G. Cvetič, *Top quark effects on the scalar sector of the minimal Standard Model*, hep-ph/9509350, Int. J. Mod. Phys. A11 (1996) 5405, 200 GeV
- [43] A. De Simone, M. P. Hertzberg & F. Wilczek, *Running Inflation in the Standard Model*, arXiv:0812.4946 [hep-ph], Phys. Lett. B 678 (2009) 1, > 126 GeV
- [44] R. Decker & J. Pestieau, *Lepton self-mass, Higgs scalar and heavy quark masses*, DESY Workshop 1979, hep-ph/0512126  
Z. Y. Fang, G. Lopez Castro, J. L. Lucio & J. Pestieau, *Effective  $SU(2)_L \times U(1)$  theory and the Higgs boson mass*, hep-ph/9612430, Mod. Phys. Lett. A12 (1997) 1531  
G. Lopez Castro & J. Pestieau, *The unit of electric charge and the mass hierarchy of heavy particles*, hep-ph/0609131, 309 GeV
- [45] A. Delgado & M. Quiros, *The lightest Higgs mass in supersymmetric models with extra dimensions*, hep-ph/0004124, Phys. Lett. B484 (2000) 355, < 165 GeV
- [46] R. Dermíšek & J. F. Gunion, *Escaping the large fine tuning and little hierarchy problems in the next to minimal supersymmetric model and  $h \rightarrow aa$  decays*, hep-ph/0502105, Phys. Rev. Lett. 95 (2005) 041801  
*Consistency of LEP event excesses with an  $h \rightarrow aa$  decay scenario and low-fine-tuning NMSSM models*, hep-ph/0510322, Phys. Rev. D73 (2006) 111701  
*The NMSSM solution to the fine-tuning problem, precision electroweak constraints*

- and the largest LEP Higgs event excess*, arXiv:0705.4387  
*A Comparison of Mixed-Higgs Scenarios In the NMSSM and the MSSM*, arXiv:0709.2269, (100 GeV)
- [47] A. Djouadi, S. Heinemeyer, M. Mondragon & G. Zoupanos, *Finite unified theories and the Higgs mass prediction*, hep-ph/0404208, 122 GeV
  - [48] M. S. El Naschie, *On Pauli's principles of "Zweiteilung und symmetrie vermin-derung" in Higgs physics and non-linear dynamics*, Chaos, Solitons & Fractals 23 (2005) 739, 161.8033989 GeV
  - [49] J. Ellis, D. Nanopoulos, K. Olive & Y. Santoso *On the Higgs mass in the CMSSM*, hep-ph/0509331, Phys. Lett. B633 (2006) 583, 120 GeV
  - [50] J. R. Espinosa & M. Quiros, *Gauge unification and the supersymmetric light Higgs mass*, hep-ph/9804235, Phys. Rev. Lett. 81 (1998) 516, < 200 GeV
  - [51] D. B. Fairlie, *Higgs field and the determination of the Weinberg angle*, Phys. Lett. B82 (1979) 97, 426 GeV
  - [52] B. Feldstein, L. J. Hall & T. Watari, *Landscape Predictions for the Higgs Boson and Top Quark Masses*, hep-ph/0608121, Phys. Rev. D74 (2006) 095011, 121 GeV
  - [53] C. D. Froggatt & H. B. Nielsen, *Standard model criticality prediction: top mass  $173 \pm 5$  GeV and Higgs mass  $135 \pm 9$  GeV*, hep-ph/9511371, Phys. Lett. B368 (1996) 96  
C. D. Froggatt, H. B. Nielsen & Y. Takanishi, *Standard model Higgs boson mass from borderline metastability of the vacuum*, hep-ph/0104161, Phys. Rev. D64 (2001) 113014, 121.8 GeV
  - [54] C. D. Froggatt, L. Laperashvili, R. Nevzorov, H. B. Nielsen & M. Sher, *Implementation of the multiple point principle in the two-Higgs doublet model of type II*, hep-ph/0602054, Phys. Rev. D73 (2006) 095005, 197.2 GeV
  - [55] C. D. Froggatt, R. Nevzorov, H. B. Nielsen & D. Thompson, *On the origin of  $Z(2)$  symmetry in the Two-Higgs Doublet extension of the SM*, arXiv:0806.3190, 200 GeV and < 125 GeV
  - [56] I. Gogoladze, T. Li & Q. Shafi, *Higgs boson mass from orbifold GUTs*, hep-ph/0602040, Phys. Rev. D73 (2006) 066008, 135 and 144 GeV
  - [57] I. Gogoladze, T. Li, V. N. Senoguz & Q. Shafi, *Higgs boson mass from orbifold GUTs with split supersymmetry*, hep-ph/0604217, Phys. Lett. B639 (2006) 332, 131 and 146 GeV
  - [58] I. Gogoladze, N. Okada & Q. Shafi, *Higgs boson mass from gauge-Higgs unification*, arXiv:0705.3035, 117 and 125 GeV

- [59] I. Gogoladze, N. Okada & Q. Shafi, *Window for Higgs boson mass from gauge-Higgs unification*, arXiv:0708.2503, 143.2 GeV
- [60] J. García-Bellido, D. G. Figueroa & J. Rubio, *Preheating in the Standard Model with the Higgs-Inflaton coupled to gravity*, arXiv:0812.4624 [hep-ph], Phys. Rev. D79 (2009) 063531, 194 GeV
- [61] B. Grzadkowski & J. F. Gunion, *Higgs-Boson Mass Limit within the Randall-Sundrum Model*, arXiv:0709.3726, < 1400 GeV
- [62] L. J. Hall & Y. Nomura, *A Finely-Predicted Higgs Boson Mass from A Finely-Tuned Weak Scale*, arXiv:0910.2235 [hep-ph], 141 GeV
- [63] Xiao-Gang He, *Higgs mass from Casimir energy induced cosmological constant in the standard model*, hep-ph/0211396, Mod. Phys. Lett. A19 (2004) 1195, 374 GeV
- [64] S. Heinemeyer, M. Mondragon & G. Zoupanos, *Confronting Finite Unified Theories with Low-Energy Phenomenology*, arXiv:0712.3630 [hep-ph] JHEP 0807 (2008) 135, 123.5 GeV
- [65] K. Huitu, P. N. Pandita & K. Puolamaki, *Mass of the lightest Higgs boson in supersymmetric left-right models*, hep-ph/9708486, Phys. Lett. B423 (1998) 97, < 446 GeV
- [66] Dae Sung Hwang, Chang-Yeong Lee & Y. Ne'eman, *BRST quantization of  $SU(2|1)$  electroweak theory in the superconnection approach and the Higgs meson mass*, Int. J. Mod. Phys. A11 (1996) 3509, 130 GeV
- [67] R. Ibáñez-Meier & P. M. Stevenson, *Autonomous renormalization of the one loop effective potential and a 2-TeV Higgs in  $SU(2) \times U(1)$* , hep-ph/9207241, Phys. Lett. B297 (1992) 144, 1900 GeV
- [68] F. Jegerlehner, M. Y. Kalmykov & O. Veretin,  *$\overline{MS}$  vs. pole masses of gauge bosons: Electroweak bosonic two-loop corrections*, hep-ph/0105304, Nucl. Phys. B641 (2002) 285  
 *$\overline{MS}$  vs pole masses of gauge bosons. II: Two-loop electroweak fermion corrections*, hep-ph/0212319, Nucl. Phys. B658 (2003) 49, < 880 GeV
- [69] T. A. Kaeding & S. Nandi, *The Higgs boson mass in gauge-mediated supersymmetry-breaking models with generalized messenger sectors*, hep-ph/9906342, < 139 GeV
- [70] P. Langacker, G. Paz, L. T. Wang & I. Yavin,  *$Z'$ -mediated Supersymmetry Breaking*, arXiv:0710.1632, 160 GeV
- [71] W. Langguth, I. Montvay & P. Weisz, *Monte Carlo Study Of The Standard  $SU(2)$  Higgs Model*, Nucl. Phys. B277 (1986) 11, 515 GeV
- [72] W. Langguth & I. Montvay, *A numerical estimate of the upper limit for the Higgs bosons mass*, Z. Phys. C36 (1987) 725, < 724 GeV

- [73] S. Litsey & M. Sher, *Higgs Masses in the Four Generation MSSM*, arXiv:0908.0502 [hep-ph], Phys. Rev. D 80 (2009) 057701, , < 400 GeV
- [74] C. Liu, *Supersymmetry for Fermion Masses*, hep-ph/0507298, Commun. Theor. Phys. 47 (2007) 1088, 145 GeV
- [75] G. López Castro & J. Pestieau, *Determination of the Higgs boson mass by the cancellation of ultraviolet divergences in the  $SU(2)_L \times U(1)$  theory*, hep-ph/9504350, Mod. Phys. Lett. A10 (1995) 1155, 308.6 GeV
- [76] R. Mahbubani, *Bounds on the Higgs mass in variations of Split Supersymmetry*, hep-ph/0408096, 255 GeV
- [77] A. Maloney, A. Pierce & J. G. Wacker, *D-terms, unification, and the Higgs mass*, hep-ph/0409127, JHEP 0606 (2006) 034, < 150 GeV
- [78] A. D. Medina, N. R. Shah & C. E. M. Wagner, *Gauge-Higgs unification and radiative electroweak symmetry breaking in warped extra dimensions*, arXiv:0706.1281, 137 GeV
- [79] T. Moroi & Y. Okada, *Upper bound of the lightest neutral Higgs mass in extended supersymmetric Standard Models*, Phys. Lett. B295 (1992) 73, < 150 and < 180 GeV
- [80] K. Namsrai, *A theoretical estimate of the Higgs boson mass*, Int. J. Theor. Phys. 35 (1996) 1369, 182 GeV
- [81] Y. Ne'eman & J. Thierry Mieg, *BRS algebra of the  $SU(2|1)$  electroweak ghost-gauge theory*, Nuov. Cim. 71A (1982) 104, 250 GeV
- [82] Y. Ne'eman, *Internal supergroup prediction of the Goldstone-Higgs particle mass*, Phys. Lett. B181 (1986) 308, 160.9 GeV
- [83] G. j. Ni, S. y. Lou, W. f. Lu & J. f. Yang,  *$\lambda \phi^4$  model and Higgs mass in standard model calculated by Gaussian effective potential approach with a new regularization-renormalization method*, hep-ph/9801264, Sci. China A41 (1998) 1206, 134 GeV
- [84] Y. Okada, M. Yamaguchi & T. Yanagida, *Upper bound of the lightest Higgs boson mass in the minimal supersymmetric standard model*, Prog. Theor. Phys. 85 (1991) 1, < 130 GeV
- [85] Y. Okumura, *An estimation of the Higgs boson mass in the two loop approximation in a noncommutative differential geometry*, hep-ph/9707350, Eur. Phys. J. C4 (1998) 711, 153 GeV
- [86] J. Pasupathy, *A calculation of Higgs mass in the standard model*, hep-ph/0006258, Mod. Phys. Lett. A15 (2000) 1605  
B. Ananthanarayan & J. Pasupathy, *Higgs mass in the standard model from coupling constant reduction*, hep-ph/0104286, Int. J. Mod. Phys. A17 (2002) 335, 154 GeV



- [87] M. Passera, W. J. Marciano & A. Sirlin, *The muon  $g-2$  and the bounds on the Higgs boson mass*, arXiv:0804.1142,  $< 130$  GeV  
M. Passera, W. J. Marciano & A. Sirlin, *The muon  $g-2$  discrepancy: new physics or a relatively light Higgs?*, arXiv:1001.4528 [hep-ph],  $< 135$  GeV
- [88] L. A. Popa, *Higgs mass from cosmological and astrophysical measurements*, arXiv:0910.5312 [astro-ph.CO], 148.1 GeV
- [89] G. Roepstorff & C. Vehn, *Towards a unified theory of gauge and Yukawa interactions*, hep-ph/0006065, 160 GeV
- [90] B. Schrempp & F. Schrempp, *An estimate for the Higgs mass*, Phys. Lett. B168 (1986) 259, 185 GeV
- [91] B. Schrempp & F. Schrempp, *A renormalization group invariant line and infrared attractive top - Higgs mass relation*, Phys. Lett. B299 (1993) 321, 155 GeV
- [92] E. Schücking, *The Higgs mass in the substandard theory*, hep-th/0702177, 115.3 GeV
- [93] M. Shaposhnikov & C. Wetterich, *Asymptotic safety of gravity and the Higgs boson mass*, arXiv:0912.0208 [hep-th], Phys. Lett. B 683 (2010) 196, 126.3 and 150 GeV
- [94] R. Squellari & C. A. Stephan, *Almost-Commutative Geometries Beyond the Standard Model III: Vector Doublets*, arXiv:0706.3112, J. Phys. A 40 (2007) 10685, 203 GeV
- [95] C. A. Stephan, *Almost-Commutative Geometries Beyond the Standard Model II: New Colours*, arXiv:0706.0595, J. Phys. A40 (2007) 9941, 241.2 GeV
- [96] D. Suematsu & G. Zoupanos,  *$\mu$ -term due to the non-universal supersymmetry breaking and the Higgs mass*, hep-ph/0102096, JHEP 0106 (2001) 038,  $< 144$  GeV
- [97] J. Tolksdorf & T. Thumstädter, *Dirac type theories and the mass of the Higgs boson*, math-ph/0602028, J. Phys. A 40 (2007) 9691, 186 GeV
- [98] R. Trostel, *Spinor connection within Weinberg-Salam model and prediction of Higgs mass*, Phys. Lett. B193 (1987) 464, 185.7 GeV
- [99] M. Veltman, *The infrared-ultraviolet connection*, Acta Phys. Polon. 12 (1981) 437, 309 GeV

CENTRE DE PHYSIQUE THÉORIQUE <sup>1</sup>  
CNRS–Luminy, Case 907  
13288 Marseille Cedex 9  
FRANCE

## Higgs-mass predictions

Thomas Schücker <sup>2</sup>

### Abstract

A compilation of Higgs-mass predictions is proposed.

PCAC-06: 14.80.Bn Standard-model Higgs boson

0708.3344

<sup>1</sup> Unité Mixte de Recherche (UMR 6207) du CNRS et des Universités Aix–Marseille 1 et 2 et Sud Toulon–Var, Laboratoire affilié à la FRUMAM (FR 2291)

<sup>2</sup> also at Université Aix–Marseille 1, [thomas.schucker@gmail.com](mailto:thomas.schucker@gmail.com)

# 1 Introduction

Many physicists hope that the electro-weak Higgs scalar will be observed within a few years at the LHC or at the Tevatron. The literature contains a plethora of predictions or upper limits of the Higgs mass based on many different ideas, models and calculational techniques. Privileged among them is the value  $m_H = 150 \pm 36$  GeV currently given by the LEP Electroweak Working Group, because it only relies on precision electro-weak data, non-observation of the Higgs today and the minimal hypothesis that the standard model is correct as it stands. A compilation of all other predictions is attempted here. Some models make additional predictions or postdictions, that are indicated. The point in time separating pre- and postdiction is taken as the time of publication of the model. In this task it is unavoidable that I will miss some references. I beg their authors' pardon and would like to ask them to kindly drop me a mail. Also some of the older post- and predictions might need an update due to changed experimental values of e.g. the top-mass, gauge couplings,... I would be happy to receive and to include such updates.

The predictions are organised in increasing order of the central value of the predicted mass interval. In a second section the upper limits are presented in increasing order as well. A third section contains a single lower limit. Older predictions and limits incompatible with today's experimental lower limit of 114 GeV are not recorded here. However, I should mention the supersymmetric model by Dermíšek & Gunion (2005) with a Higgs mass of 100 GeV. Because of exotic decay channels this model is still compatible with LEP data. Also not recorded are predictions that come with postdictions contradicting present experimental numbers.

The references are in alphabetical order of the first author's last name with chronology as secondary criterion.

## 2 Predictions

- $m_H = 109 \pm 12$  GeV

**Authors:** O. Buchmüller *et al.* (2007)

**Idea:** constrained minimal supersymmetric standard model combined with electro-weak precision data, flavor physics and abundance of cold dark matter

**Techniques:** multi-parameter fit, renormalisation group equation. The top mass is taken to be  $m_t = 170.9 \pm 1.8$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H = 115.3 \pm 0.1$  GeV

**Author:** Schücking (2007)

**Idea:** interpretation of the  $SU(2) \times U(1)$  group of the electro-weak forces as symmetry group of the Eguchi-Hanson metric

**Techniques:** differential geometry and quaternions

- $m_H = 117 \pm 4$  GeV

**Authors:** Gogoladze, Okada & Shafi (2007)

**Idea:** Higgs boson as zero mode of gauge boson along a fifth compactified dimension

**Techniques:** a boundary condition on the Higgs self-coupling at compactification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^8$  GeV

- $m_H = 118$

**Authors:** Arbuzov, Barbashov, Pervushin, Shuvalov & Zakharov (2008)

**Idea:** Three peaks of the cosmic microwave background are explained by the decay of primordial Higgs-,  $W$ - and  $Z$ -bosons into photons.

**Techniques:** conformal cosmology

**Other prediction:**  $m_H = 216$

- $m_H = 120 \pm 6$  GeV

**Authors:** Ellis, Nanopoulos, Olive & Santoso (2005)

**Idea:** supersymmetry

**Techniques:** minimal supersymmetric extension of the standard model with universal soft supersymmetry-breaking masses

**Other predictions:** many supersymmetric particles

- $m_H = 120$  GeV

**Author:** Bogan (2009)

**Idea:** simple relations between cosmological constant, GUT scale and masses of the electron, inflaton, and Higgs

**Techniques:** geometric mean

- $m_H = 121 \pm 6$  GeV

**Authors:** Feldstein, Hall & Watari (2006)

**Idea:** superstring inspired landscape of vacua and some probability density for the parameters of the Higgs potential

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{19}$  GeV

**Postdiction:**  $m_t = 176 \pm 2$  GeV

- $m_H = 121.8 \pm 11$  GeV

**Authors:** Froggatt & Nielsen (1995)

**Idea:** two approximately degenerate vacua, one in which we live, the other of Planck energy

**Techniques:** renormalisation group equations

**Postdiction:**  $m_t = 173 \pm 4$  GeV

- $m_H = 122 \pm 10$  GeV

**Authors:** Djouadi, Heinemeyer, Mondragon & Zoupanos (2004)

**Idea:** a supersymmetric version of  $SU(5)$

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

**Postdictions:**  $m_t = 174 - 183$  GeV

- $m_H = 123.5 \pm 5.5$  GeV

**Authors:** Heinemeyer, M. Mondragon & G. Zoupanos (2007)

**Idea:** a supersymmetric Grand Unified Theory that can be made all-loop finite

**Techniques:** renormalisation group flow with  $m_t = 170.9$  GeV

**Other predictions:** supersymmetric particles

- $m_H = 124 \pm 21$  GeV

**Authors:** Barger, Deshpande, Jiang, Langacker & Li (2007)

**Idea:** supersymmetry broken at  $10^5 - 10^{16}$  GeV and gauge coupling unification at  $\Lambda \sim 10^{16} - 10^{17}$  GeV

**Techniques:** renormalisation group flow up to energies of  $\Lambda$

**Other predictions:** new vectorlike fermions with masses in the 200 - 1000 GeV range

- $m_H = 124 \pm 10$  GeV

**Authors:** Arbuzov, Glinka, Lednický & Pervushin (2007), version 6

**Idea:** condensates, conformal cosmology

**Techniques:** Coleman-Weinberg potential

**Other predictions:**  $m_H = 275 \pm 25$  GeV, version 1

- $m_H = 124.2 \pm 13.2$  GeV

**Authors:** Codoban, Juncisin & Kazakov (1999)

**Idea:** supersymmetry

**Techniques:** minimal supersymmetric extension of the standard model with non-universal soft supersymmetry-breaking masses

**Other predictions:** many supersymmetric particles

- $m_H = 125 \pm 4$  GeV

**Authors:** Gogoladze, Okada & Shafi (2007)

**Idea:** Higgs boson as zero mode of gauge boson along a fifth compactified dimension

**Techniques:** a boundary condition on the Higgs self-coupling at compactification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{13} - 10^{14}$  GeV.

- $m_H = 126.3 \pm 2.2$  GeV

**Authors:** Shaposhnikov & C. Wetterich (2009)

**Idea:** Assume that gravity is asymptotically safe, that there are no intermediate energy scales between the Fermi and Planck scales, that the gravity induced anomalous dimension of the Higgs selfcoupling is positive.

**Techniques:** renormalisation group flow with  $m_t = 171.2$  GeV

- $m_H = 127.5 \pm 7.5$  GeV

**Authors:** Chankowski, Falkowski, Pokorski & Wagner (2004)

**Idea:** supersymmetry and the Higgs as a pseudo-Goldstone boson of some extra global symmetry

**Techniques:** smaller fine-tuning than in the minimal supersymmetric extension of the standard model. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 178 \pm 4.3$  GeV.

**Other predictions:** many supersymmetric particles and an additional  $Z$ -boson with a mass of 3 TeV

- $m_H = 129.6$  GeV

**Authors:** X. Calmet & H. Fritzsch (2001)

**Idea:** confining  $SU(2)$  and a ‘complementarity principle’

**Techniques:** 1-loop corrections

- $m_H = 130 \pm 6$  GeV

**Authors:** Dae Sung Hwang, Chang-Yeong Lee & Ne’eman (1996)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** renormalisation group flow

**Postdictions:**  $\sin^2 \theta_w = 0.229 \pm 0.005$

- $m_H = 131 \pm 10$  GeV

**Authors:** Gogoladze, Li, Senoguz & Shafi (2006)

**Idea:** 7 dimensional orbifold with  $SU(7)$  grand unification and split supersymmetry

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:**  $m_H = 146 \pm 8$  GeV

- $m_H = 134 \pm 9$  GeV

**Authors:** Ni, Lou, Lu & Yang (1998)

**Idea:** a Gaussian effective potential

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{15}$  GeV

- $m_H = 135 \pm 6$  GeV

**Authors:** Gogoladze, Li & Shafi (2006)

**Idea:** 7 dimensional  $N = 1$  supersymmetric orbifold with  $SU(7)$  grand unification

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:**  $m_H = 144 \pm 4$  GeV

- $m_H = 135 \pm 15$  GeV

**Authors:** Arkani-Hamed & Dimopoulos (2004)

**Idea:** split supersymmetry

**Techniques:** fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV

- $m_H = 137 \pm 23$  GeV

**Authors:** Medina, Shah & Wagner (2007)

**Idea:** a warped fifth dimension and an extension of the electro-weak gauge symmetry to  $SO(5) \times U(1)$  in the bulk, broken at the boundaries

**Techniques:** Coleman-Weinberg potential

- $m_H = 140 \pm 10$  GeV

**Authors:** Babu, Gogoladze, Rehman & Shafi (2008)

**Idea:** minimal supersymmetric extension of the standard model plus complete vectorlike multiplets of grand unified groups

**Techniques:** some fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV. The top mass is taken to be  $m_t = 172.6 \pm 1.4$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H = 141 \pm 2$  GeV

**Authors:** Hall & Y. Nomura (2009)

**Idea:** minimal supersymmetric extension of the standard model plus supersymmetry breaking at very high scale, motivated from a multiverse

**Techniques:** huge fine tuning and 2-loop corrections with a top mass of 173.1 GeV

**Other predictions:** no supersymmetric particles

- $m_H = 143 \pm 37$  GeV

**Authors:** Cabibbo, Maiani, Parisi & Petronzio (1979)

**Idea:** the big desert: no new particles besides the Higgs and validity of perturbative quantum field theory up to the Planck scale

**Techniques:** renormalisation group flow up to energies of  $10^{19}$  GeV. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 171.5 \pm 2$  GeV.

- $m_H = 143.2 \pm 28.8$  GeV

**Authors:** Gogoladze, Okada & Shafi (2007.2)

**Idea:** 2 extra dimensions compactified on an orbifold

**Techniques:** a boundary condition on the Higgs self-coupling at compactification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{19}$  GeV.

- $m_H = 144 \pm 4$  GeV

**Authors:** Gogoladze, Li & Shafi (2006)

**Idea:** 7 dimensional  $N = 1$  supersymmetric orbifold with  $SU(7)$  grand unification

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV.

**Other predictions:**  $m_H = 135 \pm 6$  GeV

- $m_H = 145 \pm 7$  GeV

**Author:** Liu (2005)

**Idea:** supersymmetry broken at  $10^{11}$  GeV and a  $\mathbb{Z}_3$  symmetry among generations

**Techniques:** radiative corrections

- $m_H = 146 \pm 8$  GeV

**Authors:** Gogoladze, Li, Senoguz & Shafi (2006)

**Idea:** 7 dimensional orbifold with  $SU(7)$  grand unification and split supersymmetry

**Techniques:** a boundary condition on the Higgs self-coupling at unification scale  $\Lambda$  and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV.

**Other predictions:**  $m_H = 131 \pm 10$  GeV

- $m_H = 146 \pm 19$  GeV

**Authors:** Barger, Jiang, Langacker & Li (2005)

**Idea:** supersymmetry broken at high scale and gauge coupling unification at  $\Lambda \sim 10^{16} - 10^{17}$  GeV

**Techniques:** renormalisation group flow up to energies of  $\Lambda$

- $m_H = 148.1 \pm 10.7$  GeV

**Author:** Popa (2009)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action with  $m_t = 171.3$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 150 \pm 36$  GeV

**Authors:** The LEP Electroweak Working Group

**Idea:** non-observation of the Higgs and quantum corrections by Higgs loops to precision electro-weak data

**Techniques:** experiment and quantum field theory

- $m_H = 150 \pm 10$  GeV

**Authors:** Barger, Chiang, Jiang & Li (2004)

**Idea:** supersymmetry broken at  $10^{11}$  GeV and Peccei-Quinn symmetry

**Techniques:** radiative corrections

- $m_H = 150 \pm 20$  GeV

**Authors:** Arvanitaki, Davis, Graham & Wacker (2004)

**Idea:** split supersymmetry

**Techniques:** fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV

- $m_H = 150 \pm 50$  GeV

**Authors:** Bai, Fan & Han (2007)

**Idea:** supersymmetry and a long-lived metastable supersymmetry breaking vacuum

**Techniques:** little Higgs mechanism, 1-loop corrections

**Other predictions:** many supersymmetric particles plus new gauge bosons and electro-weak triplets at 1 TeV

- $m_H = 150 \pm 24$  GeV

**Authors:** Shaposhnikov & C. Wetterich (2009)

**Idea:** Assume that gravity is asymptotically safe, that there are no intermediate energy scales between the Fermi and Planck scales.

**Techniques:** renormalisation group flow with  $m_t = 171.2$  GeV

- $m_H = 153 \pm 3$  GeV

**Author:** Okumura (1997)

**Idea:** a vague variant of the Connes-Lott model

**Techniques:** 2-loop renormalisation group flow up to energies of  $10^{13}$  GeV. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 171.5 \pm 2$  GeV.

- $m_H = 154 \pm 6$  GeV

**Authors:** Ananthanarayan & Pasupathy (2001)

**Idea:** weak dependence of the ratio between Higgs self-coupling and top Yukawa coupling squared on renormalisation scale

**Techniques:** 1- and 2-loop corrections

- $m_H = 154 \pm 37$  GeV

**Authors:** Gogoladze, He & Shafi (2010)

**Idea:** Vectorlike isospin doublets of quarks with masses of several 100 GeV are added to the standard model to achieve gauge unification at  $3 \cdot 10^{16}$  GeV. Assuming the validity of perturbative quantum field theory up to this energy constrains the Higgs-mass as in Cabibbo, Maiani, Parisi & Petronzio (1979).

**Techniques:** renormalisation group flow

**Other predictions:** these new vectorlike quarks



- $m_H = 154.4 \pm 0.5$  GeV

**Author:** Beck (2001)

**Idea:** ‘chaotic strings’ describing the dynamics of vacuum fluctuations underlying dark energy

**Techniques:** stochastic quantization

**Postdictions:** all fermion and gauge bosons masses, all gauge couplings

- $m_H = 155 \pm 8$  GeV

**Authors:** Schrempp & Schrempp (1993)

**Idea:** A strongly infrared attractive line in the  $m_t - m_H$  plane is found.

**Techniques:** 1-loop renormalization group equations

- $m_H = 160 \pm 8$  GeV

**Authors:** Roepstorff & Vehns (2000)

**Idea:** combining gauge and Yukawa interactions in one generalised Dirac operator

**Techniques:** superconnections

**Postdictions:**  $m_t = 160 \pm 8$  GeV

- $m_H = 160 \pm 20$  GeV

**Authors:** Langacker, Paz, Wang & Yavin (2007)

**Idea:** an extension of the minimal supersymmetric extension of the standard model plus a hidden sector plus a  $Z'$  mediating supersymmetry breaking by couplings to the hidden sector

**Techniques:** 2-loop corrections up to energies of  $10^7 - 10^{11}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H = 160 \pm 24.5$  GeV

**Authors:** Barvinsky, Kamenshchik, Kiefer, Starobinsky & Steinwachs (2009)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 1-loop with  $m_t = 171$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160 \pm 30$  GeV

**Author:** Bezrukov (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160 \pm 34$  GeV

**Authors:** Bezrukov & Shaposhnikov (2009)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 2-loop with  $m_t = 171.2$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160.7 \pm 24$  GeV

**Authors:** Bezrukov, Magnin & Shaposhnikov (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 1-loop with  $m_t = 171$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H = 160.9 \pm 0.1$  GeV

**Author:** Ne'eman (1986)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** classical field theory

**Postdictions:**  $\sin^2 \theta_w = 1/4$

- $m_H = 161.8033989$  GeV

**Author:** El Naschie (2005)

**Idea:** E-infinity theory

**Techniques:** ?

- $m_H = 170 \pm 10$  GeV

**Authors:** Chamseddine & Connes (1996)

**Idea:** derivation of the standard model from gravity by generalising Riemannian to non-commutative geometry

**Techniques:** operator algebras, heat-kernel expansion and renormalisation group flow up to energies of  $\Lambda \sim 10^{13} - 10^{17}$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 170.9 \pm 2.5$  GeV.

**Other predictions:** conceptual uncertainty in proper time measurements of  $\Delta\tau \sim \hbar/\Lambda = 10^{-41} - 10^{-37}$  s

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings,  $m_t < 186.3$  GeV.

- $m_H = 177.5 \pm 7.5$  GeV

**Authors:** Antusch, Kersten, Lindner & Ratz (2002)

**Idea:** the Higgs as a composite particle from neutrino condensation

**Techniques:** seesaw mechanism, gap equation, renormalisation group flow up to the condensation scale  $\Lambda = 10^{16}$  GeV

- $m_H = 182 \pm 4$  GeV

**Author:** Namsrai (1996)

**Idea:** Higgs mass from space-time curvature

**Techniques:** general relativity and solitons

- $m_H = 185 \pm 5$  GeV

**Author:** Schrempp & Schrempp (1986)

**Idea:** A largely unspecified strong interaction is assumed to soften the elastic scattering of longitudinally polarised  $W$  bosons.

**Techniques:** a superconvergence sum rule

- $m_H = 185.7 \pm 0.1$  GeV

**Author:** Trostel (1987)

**Idea:** a geometrisation of the Yukawa couplings

**Techniques:** spinor connections

- $m_H = 186 \pm 8$  GeV

**Authors:** Tolksdorf & Thumstädter (2006)

**Idea:** differential geometric unification of general relativity and the standard model

**Techniques:** generalised Dirac operators, heat kernel expansion and renormalisation group flow up to energies of  $\Lambda \sim 10^{10}$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 174 \pm 3$  GeV.

- $m_H = 194 \pm 80$  GeV

**Authors:** García-Bellido, Figueroa & Rubio (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background, lower limit from non-observation of the Higgs at LEP

- $m_H = 197.2 \pm 124.8$  GeV

**Authors:** Froggatt, Laperashvili, Nevzorov, Nielsen & Sher (2006)

**Idea:** non-supersymmetric extension of the standard model with two Higgs doublets and the multiple point principle

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^4 - 10^{19}$  GeV

**Other predictions:** additional neutral and charged scalars with masses larger than 202.4 GeV

- $m_H = 200 \pm 20$  GeV

**Authors:** Froggatt, Nevzorov, Nielsen & Thompson (2008)

**Idea:** non-supersymmetric extension of the standard model with two Higgs doublets and the multiple point principle

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^5$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 171.4 \pm 2.1$  GeV.

**Other predictions:** enhanced top-Higgs coupling

- $m_H = 200 \pm 50$  GeV

**Author:** Cvetič (1995)

**Idea:** It is supposed that the 1-loop contributions of the scalar self-interactions to the effective potential are distinctly less than those of the Yukawa couplings of the top.

**Techniques:** 1-loop corrections with cut-off at  $10^3$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 180$  GeV.

- $m_H = 203 \pm 2.2$  GeV

**Author:** Squellari & Stephan (2007)

**Idea:** extension of Chamseddine and Connes' spectral action to include three vectorlike isospin doublets

**Techniques:** operator algebras, heat-kernel expansion and renormalisation group flow up to  $\Lambda = 3 - 5 \cdot 10^7$  GeV. The computation of the Higgs mass depends on the top mass

taken to be  $m_t = 170.9 \pm 2.6$  GeV.

**Other predictions:** six new leptons with masses of 10–550 TeV, conceptual uncertainty in proper time measurements of  $\Delta\tau \sim \hbar/\Lambda \sim 10^{-32}$  s

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings.

- $m_H = 210 \pm 10$  GeV

**Authors:** Andrianov & Romanenko (1995)

**Idea:** modified Veltman condition and fixed point in running of Yukawa coupling

**Techniques:** renormalisation group flow up to energies of  $10^{16}$  GeV

**Postdictions:**  $m_t = 175 \pm 5$  GeV

- $m_H = 216$

**Authors:** Arbuzov, Barbashov, Pervushin, Shuvalov & Zakharov (2008)

**Idea:** Three peaks of the cosmic microwave background are explained by the decay of primordial Higgs-,  $W$ - and  $Z$ -bosons into photons.

**Techniques:** conformal cosmology

**Other prediction:**  $m_H = 118$

- $m_H = 226 \pm 50$  GeV

**Authors:** Aranda, Díaz-Cruz & Rosado (2005)

**Idea:** unification of the weak gauge couplings at intermediate energy  $\Lambda$  and linear or quadratic relation of these to the Higgs self-coupling

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{13}$  GeV

- $m_H = 241.2 \pm 1.6$  GeV

**Author:** Stephan (2007)

**Idea:** extension of Chamseddine and Connes' spectral action to  $SU(4) \times SU(3) \times SU(2) \times U(1)$

**Techniques:** operator algebras, heat-kernel expansion and renormalisation group flow up to  $\Lambda = 2 \cdot 10^4$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 170.9 \pm 2.6$  GeV.

**Other predictions:** confined  $SU(4)$  singlets in the TeV range, conceptual uncertainty in proper time measurements of  $\Delta\tau \sim \hbar/\Lambda = 3.3 \cdot 10^{-29}$  s

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings.

- $m_H = 250 \pm 50$  GeV

**Authors:** Barbieri, Hall, Nomura & Rychkov (2006)

**Idea:** extending the minimal supersymmetric extension of the standard model by adding a chiral singlet with a superpotential interaction with the Higgs doublets

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10$  TeV

- $m_H \approx 250$  GeV

**Authors:** Ne'eman & Thierry Mieg (1982)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** classical field theory

**Postdictions:**  $\sin^2 \theta_w = 1/4$

- $m_H = 255 \pm 145$  GeV

**Author:** Mahbubani (2004)

**Idea:** split supersymmetry

**Techniques:** fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV

- $m_H = 271 \pm 5$  GeV

**Authors:** Connes & Lott (1991)

**Idea:** derivation of the Higgs sector of the standard model from the Yang-Mills sector by generalising Euclidean to noncommutative geometry

**Techniques:** operator algebras. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

**Postdictions:**  $m_W^2/(\cos^2 \theta_w m_z^2) = 1$ , gluons must be massless and must have pure vector-couplings,  $m_t > 139.3$  GeV,  $\sin^2 \theta_w < 0.543$ .

- $m_H = 275 \pm 25$  GeV

**Authors:** Arbuzov, Glinka, Lednický & Pervushin (2007), version 1

**Idea:** condensates, conformal cosmology

**Techniques:** Coleman-Weinberg potential

**Other predictions:**  $m_H = 124 \pm 10$  GeV, version 6

- $m_H = 308.6 \pm 0.3$  GeV

**Authors:** López Castro & Pestieau (1995)

**Idea:** absence of quadratic and logarithmic divergences in the top mass

**Techniques:** 1-loop quantum corrections

**Other predictions:**  $m_t = 170.5 \pm 0.3$  GeV

- $m_H = 309 \pm 6$  GeV

**Authors:** Decker & Pestieau (1979), also Veltman (1981)

**Idea:** absence of quadratic 1-loop divergences

**Techniques:** dimensional reduction. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

- $m_H = 317 \pm 80$  GeV

**Authors:** Bazzocchi & Fabbrichesi (2004)

**Idea:** Flavour symmetry broken together with electro-weak symmetry, little Higgs

**Techniques:** Coleman-Weinberg effective potential

**Other predictions:** Many new particles including a charged scalar with mass  $560 \pm 192$  GeV

- $m_H = 374 \pm 6$  GeV

**Author:** Xiao-Gang He (2002)

**Idea:** no dependence of total vacuum energy (Casimir plus minimum of Higgs potential) on renormalisation scale

**Techniques:** Casimir effect and quantum corrections. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

- $m_H = 426$  GeV

**Author:** Fairlie (1979)

**Idea:** embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$

**Techniques:** classical field theory

**Postdictions:**  $\sin^2 \theta_w = 1/4$

- $m_H = 500 \pm 100$  GeV

**Authors:** Barbieri, Hall & Rychkov (2006)

**Idea:** adding an inert isospin doublet of pseudo scalars

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 1.5$  TeV

**Other predictions:** pseudo scalars with masses between 60 GeV and 1 TeV leading in particular to an increased width of the ordinary Higgs scalar

- $m_H = 515 \pm 64$  GeV

**Authors:** Langguth, Montvay & Weisz (1986)

**Idea:** lattice gauge theory and triviality of the continuum limit

**Techniques:** Monte Carlo simulations on  $12^4$  lattices

- $m_H = 536 \pm 10$  GeV

**Authors:** Babic, Guberina, Horvat & Stefancic (2001)

**Idea:** no dependence of cosmological constant on renormalisation scale

**Techniques:** quantum corrections. The computation of the Higgs mass depends on the top mass taken here to be  $m_t = 170.9 \pm 2.5$  GeV.

- $m_H = 760 \pm 21$  GeV

**Authors:** Cea, Consoli & Cosmai (2003)

**Idea:** lattice gauge theory and triviality of the continuum limit

**Techniques:** extrapolation from Ising limit

- $m_H = 1900 \pm 100$  GeV

**Authors:** Ibañez-Meier & Stevenson (1992)

**Idea:** vanishing bare Higgs mass and 1-loop effective potential

**Techniques:** autonomous renormalisation

- $m_H = 10^{18}$  GeV

**Authors:** Batakis & Kehagias (1991)

**Idea:** Higgs field as massive excitation of the vacuum configuration of a sigma field coupled to gravity

**Techniques:** non-linear sigma models

### 3 Upper bounds

- $m_H < 123$  GeV

**Authors:** Belyaev, Dar, Gogoladze, Mustafayev & Shafi (2007)

**Idea:** constrained minimal supersymmetric standard model combined with supersymmetry constraints from colliders and low energy physics and constraints on dark matter

**Techniques:** renormalisation group equation. The top mass is taken to be  $m_t = 171.4$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H < 125$  GeV

**Authors:** Froggatt, Nevzorov, Nielsen & Thompson (2008)

**Idea:** non-supersymmetric extension of the standard model with two Higgs doublets and the multiple point principle

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{10}$  GeV. The computation of the Higgs mass depends on the top mass taken to be  $m_t = 171.4 \pm 2.1$  GeV.

- $m_H < 125$  GeV

**Authors:** Babu, Gogoladze, Rehman & Shafi (2008)

**Idea:** minimal supersymmetric extension of the standard model plus complete vectorlike multiplets of grand unified groups

**Techniques:** some fine tuning and renormalisation group flow up to energies of  $10^{16}$  GeV. The top mass is taken to be  $m_t = 172.6 \pm 1.4$  GeV.

**Other predictions:** many supersymmetric particles

- $m_H < 126$  GeV

**Authors:** De Simone, Hertzberg & Wilczek (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action to 2-loop with  $m_t = 171.2$  GeV and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

- $m_H < 127$  GeV

**Authors:** Carena, Nardini, Quiros & Wagner (2008)

**Idea:** minimal supersymmetric extension of the standard model with a light stop and electro-weak baryo-genesis

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** the light stop with mass  $< 120$  GeV

- $m_H < 130$  GeV

**Authors:** Okada, Yamaguchi & Yanagida (1991)

**Idea:** minimal supersymmetric extension of the standard model

**Techniques:** soft supersymmetry breaking at 1 TeV and quantum corrections

**Other predictions:** many supersymmetric particles

- $m_H < 130$  GeV

**Authors:** Bento, Bertolami & Rosenfeld (2001)

**Idea:** introduction of a stable gauge singlet scalar of mass around 1 GeV coupled to the Higgs, playing the role of cold dark matter and solving problems with small scale structure formation

**Techniques:** phenomenological constraints from cosmology and particle physics

**Other predictions:** Higgs decay into a pair of these stable light scalars

- $m_H < 130$  GeV

**Authors:** Birkedal, Chacko & Gaillard (2004)

**Idea:** supersymmetry and the Higgs as a pseudo-Goldstone boson of some extra global symmetry

**Techniques:**  $SU(6)$  grand unification

**Other predictions:** many supersymmetric particles

- $m_H < 130$  GeV

**Authors:** Passera, Marciano & Sirlin (2008)

**Idea:** hypothetical errors in the determination of the hadronic leading-order contribution to cure the present discrepancy between experiment and prediction of the muon  $g - 2$

**Techniques:** quantum corrections by Higgs loops to precision electro-weak data with  $m_t = 172.6 \pm 1.4$  GeV

- $m_H < 139$  GeV

**Authors:** Kaeding & Nandi (1999)

**Idea:** a non-minimal supersymmetric extension of the standard model

**Techniques:** gauge mediated supersymmetry breaking and quantum corrections

**Other predictions:** many supersymmetric particles

- $m_H < 144$  GeV

**Authors:** Suematsu & Zoupanos (2001)

**Idea:** a non-minimal supersymmetric extension of the standard model

**Techniques:** non-universal soft supersymmetry breaking and quantum corrections

**Other predictions:** many supersymmetric particles

- $m_H < 150$  GeV

**Authors:** Maloney, Pierce & Wacker (2004)

**Idea:** supersymmetric extension of the standard model with non-decoupling D-terms

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles and new gauge bosons with masses in the TeV range

- $m_H < 150$  GeV

**Authors:** Moroi & Okada (1992)

**Idea:** supersymmetric extension of the standard model plus a gauge singlet

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 150$  GeV

**Authors:** Carena, Nardini, Quiros & Wagner (2008)

**Idea:** minimal supersymmetric extension of the standard model with a light stop

**Techniques:** renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** the light stop

- $m_H < 165$  GeV

**Authors:** Delgado & Quiros (2000)

**Idea:** supersymmetric extension of the standard model plus one extra dimension compactified on an orbifold

**Techniques:** renormalisation group flow with all Higgses in the bulk



**Other predictions:** many supersymmetric particles

- $m_H < 180$  GeV

**Authors:** Moroi & Okada (1992)

**Idea:** supersymmetric extension of the standard model plus extra matter multiplets

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 200$  GeV

**Authors:** Espinosa & Quiros (1998)

**Idea:** supersymmetric extension of the standard model plus extra matter multiplets

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 230$  GeV

**Authors:** Bhattacharyya, Majee & Raychaudhuri (2007)

**Idea:** supersymmetric extension of the standard model plus one extra dimension

**Techniques:** Kaluza-Klein and radiative corrections

- $m_H < 235$  GeV

**Authors:** Bhattacharyya, Majee & Ray (2008)

**Idea:** supersymmetric extension of the standard model plus one extra dimension, Higgs confined to the TeV brane

**Techniques:** Kaluza-Klein and radiative corrections

- $m_H < 260$  GeV

**Authors:** Batra, Delgado, Kaplan & Tait (2004)

**Idea:** supersymmetric extension of the standard model plus a gauge singlet

**Techniques:** soft supersymmetry breaking and renormalisation group flow up to energies of  $\Lambda \sim 10^{16}$  GeV

**Other predictions:** many supersymmetric particles and a charged Higgs boson lighter than the neutral one

- $m_H < 280$  GeV

**Authors:** Ham, Shim, Kim & Oh (2010)

**Idea:** minimal supersymmetric extension of the standard model plus a few vectorlike quarks of masses in the 300 – 550 GeV range

**Techniques:** renormalisation group flow to one-loop

**Other predictions:** many supersymmetric particles

- $m_H < 300$  GeV

**Authors:** Babu, Gogoladze & Kolda (2004)

**Idea:** minimal supersymmetric extension of the standard model plus complete vectorlike multiplets of grand unified groups

**Techniques:** renormalisation group flow up to energies of  $10^{16}$  GeV

**Other predictions:** many supersymmetric particles

- $m_H < 350$  GeV  
**Authors:** Batra, Delgado, Kaplan & Tait (2003)  
**Idea:** supersymmetric extension of the standard model plus some new gauge bosons  
**Techniques:** soft supersymmetry breaking, some fine tuning  
**Other predictions:** many supersymmetric particles and new gauge bosons with masses in the TeV range
- $m_H < 400$  GeV  
**Authors:** Litsey & M. Sher (2009)  
**Idea:** minimal supersymmetric extension of the standard model with a fourth generation  
**Techniques:** radiative corrections  
**Other predictions:** the fourth generation at LHC energies and many supersymmetric particles
- $m_H < 446$  GeV  
**Authors:** Huitu, Pandita & Puolamaki (1997)  
**Idea:** supersymmetric extension of the left-right symmetric extension of the standard model  
**Techniques:** soft supersymmetry breaking, 1-loop corrections
- $m_H < 450$  GeV  
**Authors:** Bhattacharyya, Majee & Raychaudhuri (2007)  
**Idea:** supersymmetric extension of the standard model plus two extra dimensions  
**Techniques:** Kaluza-Klein and radiative corrections
- $m_H < 724$  GeV  
**Authors:** Langguth & Montvay (1987)  
**Idea:** lattice gauge theory and triviality of the continuum limit  
**Techniques:** Monte Carlo simulations on  $16^4$  lattices
- $m_H < 800$  GeV  
**Authors:** Appelquist & Yee (2002)  
**Idea:** Kaluza-Klein with one or two extra compactified dimensions  
**Techniques:** computation of quantum corrections induced by Kaluza-Klein particles on precision electro-weak measurements of the flavour changing process  $b \rightarrow s + \gamma$  and on the anomalous magnetic moment of the muon  
**Other predictions:** new dimensions with inverse compactification radius as low as 250 GeV
- $m_H < 880$  GeV  
**Authors:** Jegerlehner, Kalmykov & Veretin (2001)  
**Idea:** Quantum corrections in the relation between  $\overline{\text{MS}}$ - and pole-masses of the  $W$ - and  $Z$ -bosons should remain perturbative.  
**Techniques:** 2-loop corrections, asymptotic expansions
- $m_H < 1008$  GeV  
**Authors:** Lee, Quigg & Thacker (1977)  
**Idea:** unitarity requirement

**Techniques:** partial-wave amplitude of elastic boson scattering in lowest order of perturbation to be bounded by unity

- $m_H < 1020$  GeV

**Authors:** Dicus & Mathur (1973)

**Idea:** unitarity requirement

**Techniques:** partial-wave amplitude of  $Z_L Z_L \rightarrow Z_L Z_L$  in lowest order of perturbation to be bounded by unity

- $m_H < 1400$  GeV

**Authors:** Grzadkowski & Gunion (2007)

**Idea:**  $W^+W^-$  scattering in the Randall-Sundrum model with one extra dimension and two 3-branes should remain perturbatively unitary after inclusion of string/M-theoretic excitations.

**Techniques:** summation of Kaluza-Klein gravitons

## 4 A lower bound

- $m_H > 230$  GeV

**Authors:** Barvinsky, Kamenshchik & Starobinsky (2008)

**Idea:** Let the Higgs be the inflaton by adding a strong, non-minimal coupling  $\varphi^2 R$  of the scalar to gravity.

**Techniques:** effective action and its confrontation with the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background

## 5 Final remarks

Our present list contains 81 Higgs-mass predictions. Supersymmetry is behind 23 of them. With the exception of two ( $250 \pm 50$  GeV,  $255 \pm 145$  GeV), their central values lie between 120 and 160 GeV. Compactified additional dimensions motivate eight predictions ranging from 117 to 146 GeV. There are two superstring inspired predictions: 121 and 154.4 GeV. The embedding of the electro-weak Lie algebra  $su(2) \oplus u(1)$  in the superalgebra  $su(2|1)$  produces four predictions: 130, 161, 250 and 426 GeV. One prediction, 178 GeV, is motivated by dynamical symmetry breaking via a neutrino condensate. We have listed four predictions from Connes's noncommutative geometry: 170, 203, 241 and 271 GeV. Lattice gauge theories lead to two predictions: 515 and 760 GeV. Eight predictions are based on the (approximate) vanishing of particular terms related to quantum corrections: 154, 155, 200, 210, 309, 374 and 536 GeV.

We have 32 upper bounds for the Higgs mass, 22 of which come from supersymmetry.

Five predictions, one upper and one lower bound come from the recent idea that inflation is driven by the Higgs scalar together with a strong non-minimal coupling to

gravity. The Higgs mass is obtained from fitting the observed spectral index and tensor-to-scalar ratio of the Cosmic Microwave Background.

The oldest entry is:  $m_H < 1020$  GeV by Dicus & Mathur (1973).

The most precise prediction is:  $m_H = 161.8033989$  GeV by El Naschie (2005).

The highest prediction is:  $m_H = 10^{18}$  GeV by Batakis & Kehagias (1991).

The highest number of predictions by a single co-author, Gogoladze, is 12.

The following three intervals are still free of Higgs-mass predictions:

600 – 739 GeV, 781 – 1800 GeV and 2000 –  $10^{18}$  GeV.

In this compilation we have only considered numerical post- and predictions. Today particle physicists are used to interpret experimental numbers not only in terms of numbers like coupling constants, but also in terms of groups and representations and even in terms of Lagrangians. Only few of the listed models come with constraints on groups, representations and Lagrangians. Supersymmetric models for instance need representations for supersymmetric particles and thereby may be falsified by the LHC. However supersymmetry does not constrain the gauge group nor the Lagrangian. This is different for Connes' noncommutative geometry, which — just as Riemannian geometry — puts severe constraints on the admissible Lagrangians, puts constraints on gauge groups and severe constraints on representations. In particular the Higgs representation of the noncommutative standard model is not chosen but computed to be one colourless isospin doublet. This is certainly its most startling and robust prediction and may lead to its falsification if more than one physical Higgs is found as predicted by any supersymmetric standard model.

## References

- [1] The LEP Electroweak Working Group, <http://lepewwg.web.cern.ch>, 150 GeV
- [2] A. A. Andrianov & N. V. Romanenko, *Vacuum Fine Tuning And Masses Of The T Quark And Higgs Boson*, Phys. Lett. B343 (1995) 295, 210 GeV
- [3] S. Antusch, J. Kersten, M. Lindner & M. Ratz, *Dynamical electroweak symmetry breaking by a neutrino condensate*, hep-ph/0211385, Nucl. Phys. B658 (2003) 203, 177.5 GeV
- [4] T. Appelquist & Ho-Ung Yee, *Universal extra dimensions and the Higgs boson mass*, hep-ph/0211023, Phys. Rev. D67 (2003) 055002, < 800 GeV
- [5] A. Aranda, J. L. Díaz-Cruz & A. Rosado, *Electroweak-Higgs unification and the Higgs boson mass*, hep-ph/0507230, Int. J. Mod. Phys. A22 (2007) 1417, 226 GeV
- [6] A. B. Arbuzov, L. A. Glinka, R. Lednicky & V. N. Pervushin, *Higgs Particle Mass in Cosmology*, arXiv:0705.4672, 124 and 275 GeV
- [7] A. B. Arbuzov, B. M. Barbashov, V. N. Pervushin, S. A. Shuvalov & A. F. Zakharov, *Is it possible to estimate the Higgs Mass from the CMB Power Spectrum?*, arXiv:0802.3427, 118 and 216 GeV

- [8] N. Arkani-Hamed & S. Dimopoulos, *Supersymmetric unification without low energy supersymmetry and signatures for fine-tuning at the LHC*, hep-th/0405159, JHEP 0506 (2005) 073, 135 GeV
- [9] A. Arvanitaki, C. Davis, P. W. Graham & J. G. Wacker, *One loop predictions of the finely tuned SSM*, hep-ph/0406034, Phys. Rev. D70 (2004) 117703, 150 GeV
- [10] A. Babic, B. Guberina, R. Horvat & H. Stefancic, *Renormalization-group running of the cosmological constant and its implication for the Higgs boson mass in the standard model*, hep-ph/0111207 Phys. Rev. D65 (2002) 085002, 536 GeV
- [11] K. S. Babu, I. Gogoladze & C. Kolda, *Perturbative unification and Higgs boson mass bounds*, arXiv:hep-ph/0410085,  $< 300$  GeV
- [12] K. S. Babu, I. Gogoladze, M. U. Rehman & Q. Shafi, *Higgs Boson Mass, Sparticle Spectrum and Little Hierarchy Problem in Extended MSSM*, arXiv:0807.3055, 140 GeV,  $< 125$  GeV
- [13] Y. Bai, J. Fan & Z. Han, *Higgs boson from the meta-stable SUSY breaking sector*, arXiv:0706.0007, 150 GeV
- [14] R. Barbieri, L. J. Hall & V. S. Rychkov, *Improved naturalness with a heavy Higgs: An alternative road to LHC physics*, hep-ph/0603188, Phys. Rev. D74 (2006) 015007, 500 GeV
- [15] R. Barbieri, L. J. Hall, Y. Nomura & V. S. Rychkov, *Supersymmetry without a light Higgs boson*, hep-ph/0607332, Phys. Rev. D75 (2007) 035007, 250 GeV
- [16] V. Barger, C. W. Chiang, J. Jiang & T. Li, *Axion models with high-scale supersymmetry breaking*, hep-ph/0410252, Nucl. Phys. B705 (2005) 71, 150 GeV
- [17] V. Barger, J. Jiang, P. Langacker & T. Li, *Gauge coupling unification in the standard model*, hep-ph/0503226, Phys. Lett. B624 (2005) 233  
*Non-canonical gauge coupling unification in high-scale supersymmetry breaking*, hep-ph/0504093, Nucl. Phys. B726 (2005) 149, 146 GeV
- [18] V. Barger, N. G. Deshpande, J. Jiang, P. Langacker & T. Li, *Implications of canonical gauge coupling unification in high-scale supersymmetry breaking*, hep-ph/0701136, 124 GeV
- [19] A. O. Barvinsky, A. Y. Kamenshchik & A. A. Starobinsky, *Inflation scenario via the Standard Model Higgs boson and LHC*, arXiv:0809.2104 [hep-ph], JCAP 0811 (2008) 021,  $> 230$  GeV
- [20] A. O. Barvinsky, A. Y. Kamenshchik, C. Kiefer, A. A. Starobinsky & C. Steinwachs, *Asymptotic freedom in inflationary cosmology with a non-minimally coupled Higgs field*, arXiv:0904.1698 [hep-ph], JCAP 0912 (2009) 003, 160 GeV

- [21] N. A. Batakis & A. A. Kehagias, *Higgs mass determined in the gravity coupled sigma model*, Phys. Lett. B253 (1991) 149,  $10^{18}$  GeV
- [22] P. Batra, A. Delgado, D. E. Kaplan & T. M. P. Tait, *The Higgs mass bound in gauge extensions of the minimal supersymmetric standard model*, hep-ph/0309149, JHEP 0402 (2004) 043,  $< 350$  GeV
- [23] P. Batra, A. Delgado, D. E. Kaplan & T. M. P. Tait, *Running into new territory in SUSY parameter space*, hep-ph/0404251, JHEP 0406 (2004) 032,  $< 260$  GeV
- [24] F. Bazzocchi & M. Fabbrichesi, *A Heavy Higgs boson from flavor and electroweak symmetry breaking unification*, hep-ph/0407358, Phys. Rev. D70 (2004) 115008, 317 GeV
- [25] C. Beck, *Chaotic strings and standard model parameters*, hep-th/0105152, Physica D 171 (2002) 72, 154.4 GeV
- [26] A. Belyaev, S. Dar, I. Gogoladze, A. Mustafayev & Q. Shafi, *Interplay of Higgs and Sparticle Masses in the CMSSM with updated SUSY constraints*, arXiv:0712.1049,  $< 123$  GeV
- [27] M. C. Bento, O. Bertolami & R. Rosenfeld, *Cosmological constraints on an invisibly decaying Higgs boson*, hep-ph/0103340, Phys. Lett. B518 (2001) 276,  $< 130$  GeV
- [28] F. L. Bezrukov, *The Standard model Higgs as the inflaton*, arXiv:0805.2236 [hep-ph], 160 GeV
- [29] F. L. Bezrukov, A. Magnin & M. Shaposhnikov, *Standard Model Higgs boson mass from inflation*, arXiv:0812.4950 [hep-ph], Phys. Lett. B 675 (2009) 88, 160.7 GeV
- [30] F. Bezrukov & M. Shaposhnikov, *Standard Model Higgs boson mass from inflation: two loop analysis*, arXiv:0904.1537 [hep-ph], JHEP 0907 (2009) 089, 160 GeV
- [31] G. Bhattacharyya, S. K. Majee & A. Raychaudhuri, *Extra-dimensional relaxation of the upper limit of the lightest supersymmetric neutral Higgs mass*, arXiv:0705.3103,  $< 230$  and  $< 450$  GeV
- [32] G. Bhattacharyya, S. K. Majee & T. S. Ray, *Radiative correction to the lightest neutral Higgs mass in warped supersymmetry*, arXiv:0806.3672,  $< 235$  GeV
- [33] A. Birkedal, Z. Chacko & M. K. Gaillard, *Little supersymmetry and the supersymmetric little hierarchy problem*, hep-ph/0404197, JHEP 0410 (2004) 036,  $< 130$  GeV
- [34] J. R. Bogan, *From the Cosmological Constant: Higgs Boson, Quantum Gravity, and Horizon Scales*, arXiv:0902.2600 [physics.gen-ph], 120 GeV
- [35] O. Buchmüller *et al.*, *Prediction for the Lightest Higgs Boson Mass in the CMSSM using Indirect Experimental Constraints*, arXiv:0707.3447, Phys. Lett. B657 (2007) 87, 109 GeV

- [36] N. Cabibbo, L. Maiani, G. Parisi & R. Petronzio, *Bounds on the fermions and Higgs boson masses in grand unified theories*, Nucl. Phys. B158 (1979) 295, 143 GeV
- [37] X. Calmet & H. Fritzsch, *Calculation of the Higgs boson mass using the complementarity principle*, hep-ph/0107085, Phys. Lett. B525 (2002) 297, 129.6 GeV
- [38] M. Carena, G. Nardini, M. Quiros & C. E. M. Wagner, *The Effective Theory of the Light Stop Scenario*, arXiv:0806.4297, JHEP 0810 (2008) 062, < 150 GeV
- [39] M. Carena, G. Nardini, M. Quiros & C. E. M. Wagner, *The Baryogenesis Window in the MSSM*, arXiv:0809.3760, Nucl. Phys. B812 (2009) 243, < 127 GeV
- [40] P. Cea, M. Consoli & L. Cosmai, *Indications on the Higgs boson mass from lattice simulations*, hep-lat/0309050 Nucl. Phys. Proc. Suppl. 129 (2004) 780, 760 GeV  
P. Cea & L. Cosmai, *The Higgs boson: from the lattice to LHC*, arXiv:0911.5220 [hep-ph], 754 GeV
- [41] A. Chamseddine & A. Connes, *The spectral action principle*, hep-th/9606001, Comm. Math. Phys. 182 (1996) 155  
A. Chamseddine, A. Connes & M. Marcolli, *Gravity and the standard model with neutrino mixing*, hep-th/0610241, Adv. Theor. Math. Phys. 11 (2007) 991, 170 GeV
- [42] P. H. Chankowski, A. Falkowski, S. Pokorski & J. Wagner, *Electroweak symmetry breaking in supersymmetric models with heavy scalar superpartners*, hep-ph/0407242, Phys. Lett. B598 (2004) 252, 127.5 GeV
- [43] S. Codoban, M. Juncisin & D. Kazakov, *Higgs mass prediction with non-universal soft supersymmetry breaking in MSSM*, hep-ph/9912504, Phys. Lett. B477 (2000) 223, 124.2 GeV
- [44] A. Connes & J. Lott, *The metric aspect of noncommutative geometry*, in the proceedings of the 1991 Cargèse Summer Conference, eds.: J. Fröhlich et al., Plenum Press (1992)  
D. Kastler & T. Schücker, *The standard model à la Connes-Lott*, hep-th/9412185, J. Geom. Phys. 24 (1997) 1, 271 GeV
- [45] G. Cvetič, *Top quark effects on the scalar sector of the minimal Standard Model*, hep-ph/9509350, Int. J. Mod. Phys. A11 (1996) 5405, 200 GeV
- [46] A. De Simone, M. P. Hertzberg & F. Wilczek, *Running Inflation in the Standard Model*, arXiv:0812.4946 [hep-ph], Phys. Lett. B 678 (2009) 1, > 126 GeV
- [47] R. Decker & J. Pestieau, *Lepton self-mass, Higgs scalar and heavy quark masses*, DESY Workshop 1979, hep-ph/0512126  
Z. Y. Fang, G. Lopez Castro, J. L. Lucio & J. Pestieau, *Effective  $SU(2)_L \times U(1)$  theory and the Higgs boson mass*, hep-ph/9612430, Mod. Phys. Lett. A12 (1997) 1531  
G. Lopez Castro & J. Pestieau, *The unit of electric charge and the mass hierarchy of heavy particles*, hep-ph/0609131, 309 GeV

- [48] A. Delgado & M. Quiros, *The lightest Higgs mass in supersymmetric models with extra dimensions*, hep-ph/0004124, Phys. Lett. B484 (2000) 355,  $< 165$  GeV
- [49] R. Dermíšek & J. F. Gunion, *Escaping the large fine tuning and little hierarchy problems in the next to minimal supersymmetric model and  $h \rightarrow aa$  decays*, hep-ph/0502105, Phys. Rev. Lett. 95 (2005) 041801  
*Consistency of LEP event excesses with an  $h \rightarrow aa$  decay scenario and low-fine-tuning NMSSM models*, hep-ph/0510322, Phys. Rev. D73 (2006) 111701  
*The NMSSM solution to the fine-tuning problem, precision electroweak constraints and the largest LEP Higgs event excess*, arXiv:0705.4387  
*A Comparison of Mixed-Higgs Scenarios In the NMSSM and the MSSM*, arXiv:0709.2269, (100 GeV)
- [50] D. A. Dicus & V. S. Mathur, *Upper Bounds On The Values Of Masses In Unified Gauge Theories*, Phys. Rev. D7 (1973) 3111,  $< 1020$  GeV
- [51] A. Djouadi, S. Heinemeyer, M. Mondragon & G. Zoupanos, *Finite unified theories and the Higgs mass prediction*, hep-ph/0404208, 122 GeV
- [52] M. S. El Naschie, *On Pauli's principles of "Zweiteilung und symmetrie vermin-derung" in Higgs physics and non-linear dynamics*, Chaos, Solitons & Fractals 23 (2005) 739, 161.8033989 GeV
- [53] J. Ellis, D. Nanopoulos, K. Olive & Y. Santoso *On the Higgs mass in the CMSSM*, hep-ph/0509331, Phys. Lett. B633 (2006) 583, 120 GeV
- [54] J. R. Espinosa & M. Quiros, *Gauge unification and the supersymmetric light Higgs mass*, hep-ph/9804235, Phys. Rev. Lett. 81 (1998) 516,  $< 200$  GeV
- [55] D. B. Fairlie, *Higgs field and the determination of the Weinberg angle*, Phys. Lett. B82 (1979) 97, 426 GeV
- [56] B. Feldstein, L. J. Hall & T. Watari, *Landscape Predictions for the Higgs Boson and Top Quark Masses*, hep-ph/0608121, Phys. Rev. D74 (2006) 095011, 121 GeV
- [57] C. D. Froggatt & H. B. Nielsen, *Standard model criticality prediction: top mass  $173 \pm 5$  GeV and Higgs mass  $135 \pm 9$  GeV*, hep-ph/9511371, Phys. Lett. B368 (1996) 96  
C. D. Froggatt, H. B. Nielsen & Y. Takanishi, *Standard model Higgs boson mass from borderline metastability of the vacuum*, hep-ph/0104161, Phys. Rev. D64 (2001) 113014, 121.8 GeV
- [58] C. D. Froggatt, L. Laperashvili, R. Nevzorov, H. B. Nielsen & M. Sher, *Implementation of the multiple point principle in the two-Higgs doublet model of type II*, hep-ph/0602054, Phys. Rev. D73 (2006) 095005, 197.2 GeV
- [59] C. D. Froggatt, R. Nevzorov, H. B. Nielsen & D. Thompson, *On the origin of  $Z(2)$  symmetry in the Two-Higgs Doublet extension of the SM*, arXiv:0806.3190, 200 GeV and  $< 125$  GeV



- [60] I. Gogoladze, T. Li & Q. Shafi, *Higgs boson mass from orbifold GUTs*, hep-ph/0602040, Phys. Rev. D73 (2006) 066008, 135 and 144 GeV
- [61] I. Gogoladze, T. Li, V. N. Senoguz & Q. Shafi, *Higgs boson mass from orbifold GUTs with split supersymmetry*, hep-ph/0604217, Phys. Lett. B639 (2006) 332, 131 and 146 GeV
- [62] I. Gogoladze, N. Okada & Q. Shafi, *Higgs boson mass from gauge-Higgs unification*, arXiv:0705.3035, 117 and 125 GeV
- [63] I. Gogoladze, N. Okada & Q. Shafi, *Window for Higgs boson mass from gauge-Higgs unification*, arXiv:0708.2503, 143.2 GeV
- [64] I. Gogoladze, B. He & Q. Shafi, *New Fermions at the LHC and Mass of the Higgs Boson*, arXiv:1004.4217 [hep-ph], 154 GeV
- [65] J. García-Bellido, D. G. Figueroa & J. Rubio, *Preheating in the Standard Model with the Higgs-Inflaton coupled to gravity*, arXiv:0812.4624 [hep-ph], Phys. Rev. D79 (2009) 063531, 194 GeV
- [66] B. Grzadkowski & J. F. Gunion, *Higgs-Boson Mass Limit within the Randall-Sundrum Model*, arXiv:0709.3726, < 1400 GeV
- [67] L. J. Hall & Y. Nomura, *A Finely-Predicted Higgs Boson Mass from A Finely-Tuned Weak Scale*, arXiv:0910.2235 [hep-ph], 141 GeV
- [68] S. W. Ham, S. A. Shim, C. M. Kim & S. K. Oh, *Higgs boson masses in an extension of the MSSM with vectorlike quarks*, arXiv:1004.1974 [hep-ph], < 280 GeV
- [69] Xiao-Gang He, *Higgs mass from Casimir energy induced cosmological constant in the standard model*, hep-ph/0211396, Mod. Phys. Lett. A19 (2004) 1195, 374 GeV
- [70] S. Heinemeyer, M. Mondragon & G. Zoupanos, *Confronting Finite Unified Theories with Low-Energy Phenomenology*, arXiv:0712.3630 [hep-ph] JHEP 0807 (2008) 135, 123.5 GeV
- [71] K. Huitu, P. N. Pandita & K. Puolamaki, *Mass of the lightest Higgs boson in supersymmetric left-right models*, hep-ph/9708486, Phys. Lett. B423 (1998) 97, < 446 GeV
- [72] Dae Sung Hwang, Chang-Yeong Lee & Y. Ne'eman, *BRST quantization of  $SU(2|1)$  electroweak theory in the superconnection approach and the Higgs meson mass*, Int. J. Mod. Phys. A11 (1996) 3509, 130 GeV
- [73] R. Ibañez-Meier & P. M. Stevenson, *Autonomous renormalization of the one loop effective potential and a 2-TeV Higgs in  $SU(2) \times U(1)$* , hep-ph/9207241, Phys. Lett. B297 (1992) 144, 1900 GeV

- [74] F. Jegerlehner, M. Y. Kalmykov & O. Veretin, *MS-bar vs. pole masses of gauge bosons: Electroweak bosonic two-loop corrections*, hep-ph/0105304, Nucl. Phys. B641 (2002) 285  
*MS-bar vs pole masses of gauge bosons. II: Two-loop electroweak fermion corrections*, hep-ph/0212319, Nucl. Phys. B658 (2003) 49, < 880 GeV
- [75] T. A. Kaeding & S. Nandi, *The Higgs boson mass in gauge-mediated supersymmetry-breaking models with generalized messenger sectors*, hep-ph/9906342, < 139 GeV
- [76] P. Langacker, G. Paz, L. T. Wang & I. Yavin, *Z'-mediated Supersymmetry Breaking*, arXiv:0710.1632, 160 GeV
- [77] W. Langguth, I. Montvay & P. Weisz, *Monte Carlo Study Of The Standard SU(2) Higgs Model*, Nucl. Phys. B277 (1986) 11, 515 GeV
- [78] W. Langguth & I. Montvay, *A numerical estimate of the upper limit for the Higgs bosons mass*, Z. Phys. C36 (1987) 725, < 724 GeV
- [79] B. W. Lee, C. Quigg & H. B. Thacker, *Weak Interactions At Very High-Energies: The Role Of The Higgs Boson Mass*, Phys. Rev. D16 (1977) 1519, < 1008 GeV
- [80] S. Litsey & M. Sher, *Higgs Masses in the Four Generation MSSM*, arXiv:0908.0502 [hep-ph], Phys. Rev. D 80 (2009) 057701, , < 400 GeV
- [81] C. Liu, *Supersymmetry for Fermion Masses*, hep-ph/0507298, Commun. Theor. Phys. 47 (2007) 1088, 145 GeV
- [82] G. López Castro & J. Pestieau, *Determination of the Higgs boson mass by the cancellation of ultraviolet divergences in the SU(2)<sub>L</sub> × U(1) theory*, hep-ph/9504350, Mod. Phys. Lett. A10 (1995) 1155, 308.6 GeV
- [83] R. Mahbubani, *Bounds on the Higgs mass in variations of Split Supersymmetry*, hep-ph/0408096, 255 GeV
- [84] A. Maloney, A. Pierce & J. G. Wacker, *D-terms, unification, and the Higgs mass*, hep-ph/0409127, JHEP 0606 (2006) 034, < 150 GeV
- [85] A. D. Medina, N. R. Shah & C. E. M. Wagner, *Gauge-Higgs unification and radiative electroweak symmetry breaking in warped extra dimensions*, arXiv:0706.1281, 137 GeV
- [86] T. Moroi & Y. Okada, *Upper bound of the lightest neutral Higgs mass in extended supersymmetric Standard Models*, Phys. Lett. B295 (1992) 73, < 150 and < 180 GeV
- [87] K. Namsrai, *A theoretical estimate of the Higgs boson mass*, Int. J. Theor. Phys. 35 (1996) 1369, 182 GeV

- [88] Y. Ne'eman & J. Thierry Mieg, *BRS algebra of the  $SU(2|1)$  electroweak ghost-gauge theory*, Nuov. Cim. 71A (1982) 104, 250 GeV
- [89] Y. Ne'eman, *Internal supergroup prediction of the Goldstone-Higgs particle mass*, Phys. Lett. B181 (1986) 308, 160.9 GeV
- [90] G. j. Ni, S. y. Lou, W. f. Lu & J. f. Yang,  *$\lambda \phi^4$  model and Higgs mass in standard model calculated by Gaussian effective potential approach with a new regularization-renormalization method*, hep-ph/9801264, Sci. China A41 (1998) 1206, 134 GeV
- [91] Y. Okada, M. Yamaguchi & T. Yanagida, *Upper bound of the lightest Higgs boson mass in the minimal supersymmetric standard model*, Prog. Theor. Phys. 85 (1991) 1, < 130 GeV
- [92] Y. Okumura, *An estimation of the Higgs boson mass in the two loop approximation in a noncommutative differential geometry*, hep-ph/9707350, Eur. Phys. J. C4 (1998) 711, 153 GeV
- [93] J. Pasupathy, *A calculation of Higgs mass in the standard model*, hep-ph/0006258, Mod. Phys. Lett. A15 (2000) 1605  
B. Ananthanarayan & J. Pasupathy, *Higgs mass in the standard model from coupling constant reduction*, hep-ph/0104286, Int. J. Mod. Phys. A17 (2002) 335, 154 GeV
- [94] M. Passera, W. J. Marciano & A. Sirlin, *The muon  $g-2$  and the bounds on the Higgs boson mass*, arXiv:0804.1142, < 130 GeV  
M. Passera, W. J. Marciano & A. Sirlin, *The muon  $g-2$  discrepancy: new physics or a relatively light Higgs?*, arXiv:1001.4528 [hep-ph], < 135 GeV
- [95] L. A. Popa, *Higgs mass from cosmological and astrophysical measurements*, arXiv:0910.5312 [astro-ph.CO], 148.1 GeV
- [96] G. Roepstorff & C. Vehns, *Towards a unified theory of gauge and Yukawa interactions*, hep-ph/0006065, 160 GeV
- [97] B. Schrempp & F. Schrempp, *An estimate for the Higgs mass*, Phys. Lett. B168 (1986) 259, 185 GeV
- [98] B. Schrempp & F. Schrempp, *A renormalization group invariant line and infrared attractive top - Higgs mass relation*, Phys. Lett. B299 (1993) 321, 155 GeV
- [99] E. Schücking, *The Higgs mass in the substandard theory*, hep-th/0702177, 115.3 GeV
- [100] M. Shaposhnikov & C. Wetterich, *Asymptotic safety of gravity and the Higgs boson mass*, arXiv:0912.0208 [hep-th], Phys. Lett. B 683 (2010) 196, 126.3 and 150 GeV

- [101] R. Squellari & C. A. Stephan, *Almost-Commutative Geometries Beyond the Standard Model III: Vector Doublets*, arXiv:0706.3112 , J. Phys. A 40 (2007) 10685, 203 GeV
- [102] C. A. Stephan, *Almost-Commutative Geometries Beyond the Standard Model II: New Colours*, arXiv:0706.0595, J. Phys. A40 (2007) 9941, 241.2 GeV
- [103] D. Suematsu & G. Zoupanos,  *$\mu$ -term due to the non-universal supersymmetry breaking and the Higgs mass*, hep-ph/0102096, JHEP 0106 (2001) 038, < 144 GeV
- [104] J. Tolksdorf & T. Thumstädter, *Dirac type theories and the mass of the Higgs boson*, math-ph/0602028, J. Phys. A 40 (2007) 9691, 186 GeV
- [105] R. Trostel, *Spinor connection within Weinberg-Salam model and prediction of Higgs mass*, Phys. Lett. B193 (1987) 464, 185.7 GeV
- [106] M. Veltman, *The infrared-ultraviolet connection*, Acta Phys. Polon. 12 (1981) 437, 309 GeV